

# ECE171A: Linear Control System Theory Discussion

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## MATLAB Polynomial Functions

- ▶ Consider:

$$p(s) = (s - 11.6219)(s + 0.3110 + 2.6704j)(s + 0.3110 - 2.6704j)$$

- ▶ poly: convert roots to polynomial coefficients:

```
1 r = [11.6219, -0.3110-2.6704i, -0.3110+2.6704i]
  a = poly(r) = [1.0, -11.0, 0.0, -84.0]
```

- ▶ polyval: evaluate a polynomial, e.g.,  $p(1 - 2j)$ :

```
polyval(a, 1-2i) = -62 + 46i
```

- ▶ roots: find polynomial roots:

```
1 roots(a) = [11.6219, -0.3110-2.6704i, -0.3110+2.6704i]
```

- ▶ conv: expand the product of two polynomials, e.g.,  $(3s^2 + 2s + 1)(s + 4)$ :

```
1 conv([3, 2, 1], [1, 4]) = [3, 14, 9, 4]
```

## MATLAB Control System Functions

- ▶  $SYS = tf(NUM,DEN)$ : creates a continuous-time transfer function  $SYS$  with numerator  $NUM$  and denominator  $DEN$ :

```
1 dcmotor = tf(200,[1 1]);
```

- ▶  $SYS = series(SYS1,SYS2)$ : series connection of  $SYS1$  and  $SYS2$ :

```
1 fwdsys = series(tf(200,[1 1]), tf(1,[1 8]));
```

- ▶  $SYS = parallel(SYS1,SYS2)$ : parallel connection of  $SYS1$  and  $SYS2$

```
1 fwdsys = parallel(tf(200,[1 1]), tf(1,[1 8]));
```

- ▶  $SYS = feedback(SYS1, SYS2, sign)$ : feedback connection of  $SYS1$  and  $SYS2$ :

```
1 fbksys = feedback(series(tf(200,[1 1]), tf(1,[1 8])),tf(1,[0.25 1]))
```

## MATLAB Control System Functions

- ▶  $SYS = \text{zpk}(Z,P,K)$  creates a continuous-time zero-pole-gain (zpk) model  $SYS$  with zeros  $Z$ , poles  $P$ , and gains  $K$ :

```
1 dcmotor = zpk([], [-1], 200);  
  fbksys = zpk([-4], [-8.8426, -2.0787 + 1.7078i, -2.0787 -1.7078i], 8);
```

- ▶  $P = \text{pole}(SYS)$  returns the poles  $P$  of  $SYS$ :

```
sp = pole(fbksys) = [-8.8426, -2.0787 + 1.7078i, -2.0787 -1.7078i]
```

- ▶  $[Z,G] = \text{zero}(SYS)$  computes the zeros  $Z$  and gain  $G$  of  $SYS$ :

```
1 [sz,k] = zero(fbksys) = [-4, 8]
```

- ▶  $\text{pzmap}(SYS)$ : computes and plots the poles and zeros of  $SYS$

```
1 pzmap(fbksys)
```

## MATLAB Control System Functions

- ▶  $Y = \text{step}(\text{SYS}, T)$ : computes the step response  $Y$  of  $\text{SYS}$  at times  $T$

```
1 t = 0:0.01:5;  
  step(fbksys,t);
```

- ▶  $Y = \text{impulse}(\text{SYS}, T)$ : computes the impulse response  $Y$  of  $\text{SYS}$  at times  $T$

```
2 t = 0:0.01:5;  
  impulse(fbksys,t);
```

- ▶  $Y = \text{lsim}(\text{SYS}, U, T)$ : computes the output response  $Y$  of  $\text{SYS}$  with input  $U$  at times  $T$

```
2 [u,t] = gensig('square',4,10,0.1);  
  lsim(fbksys,u,t);
```