

# ECE276A: Sensing & Estimation in Robotics

## Lecture 1: Introduction

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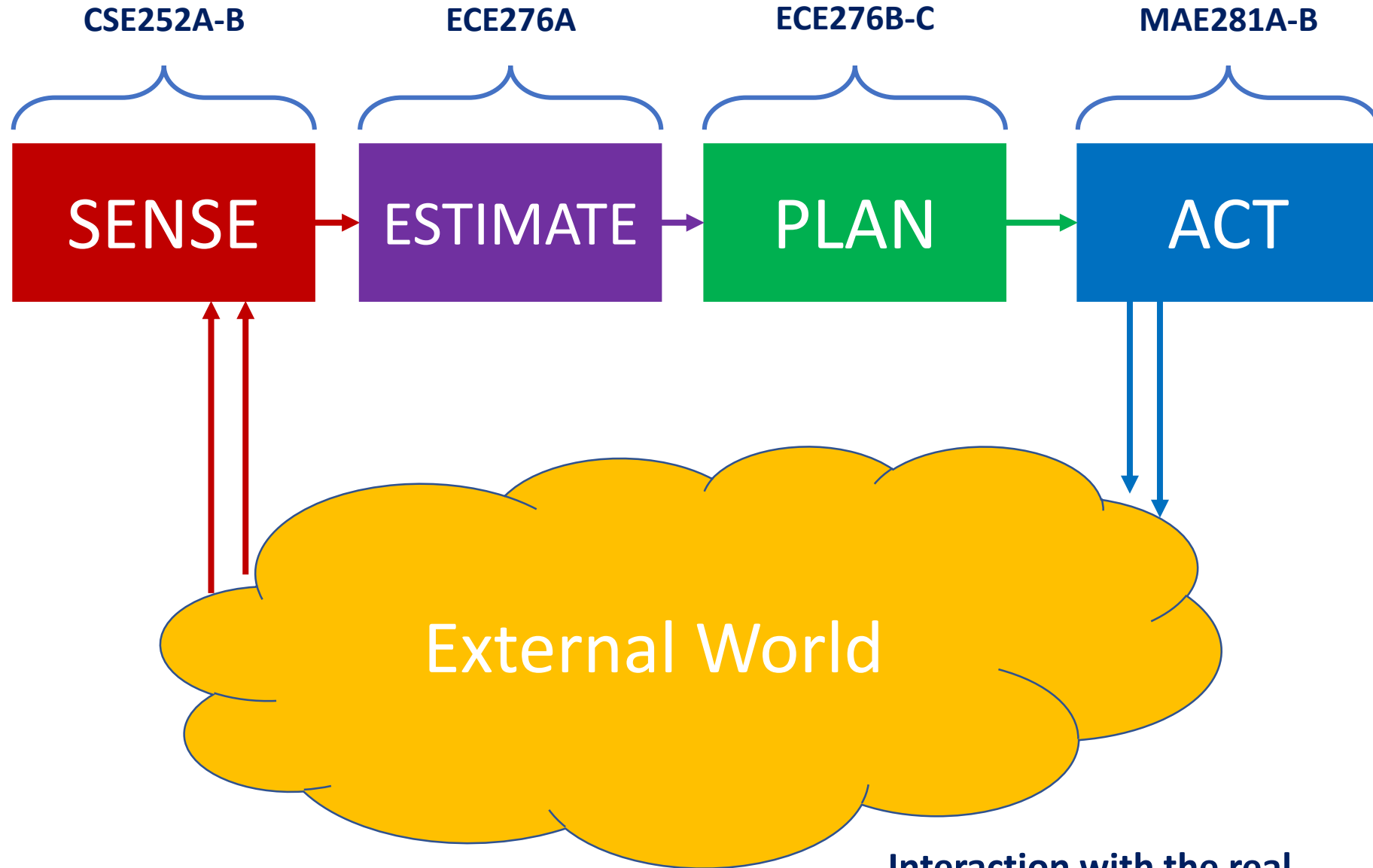
**UC San Diego**

**JACOBS SCHOOL OF ENGINEERING**  
Electrical and Computer Engineering

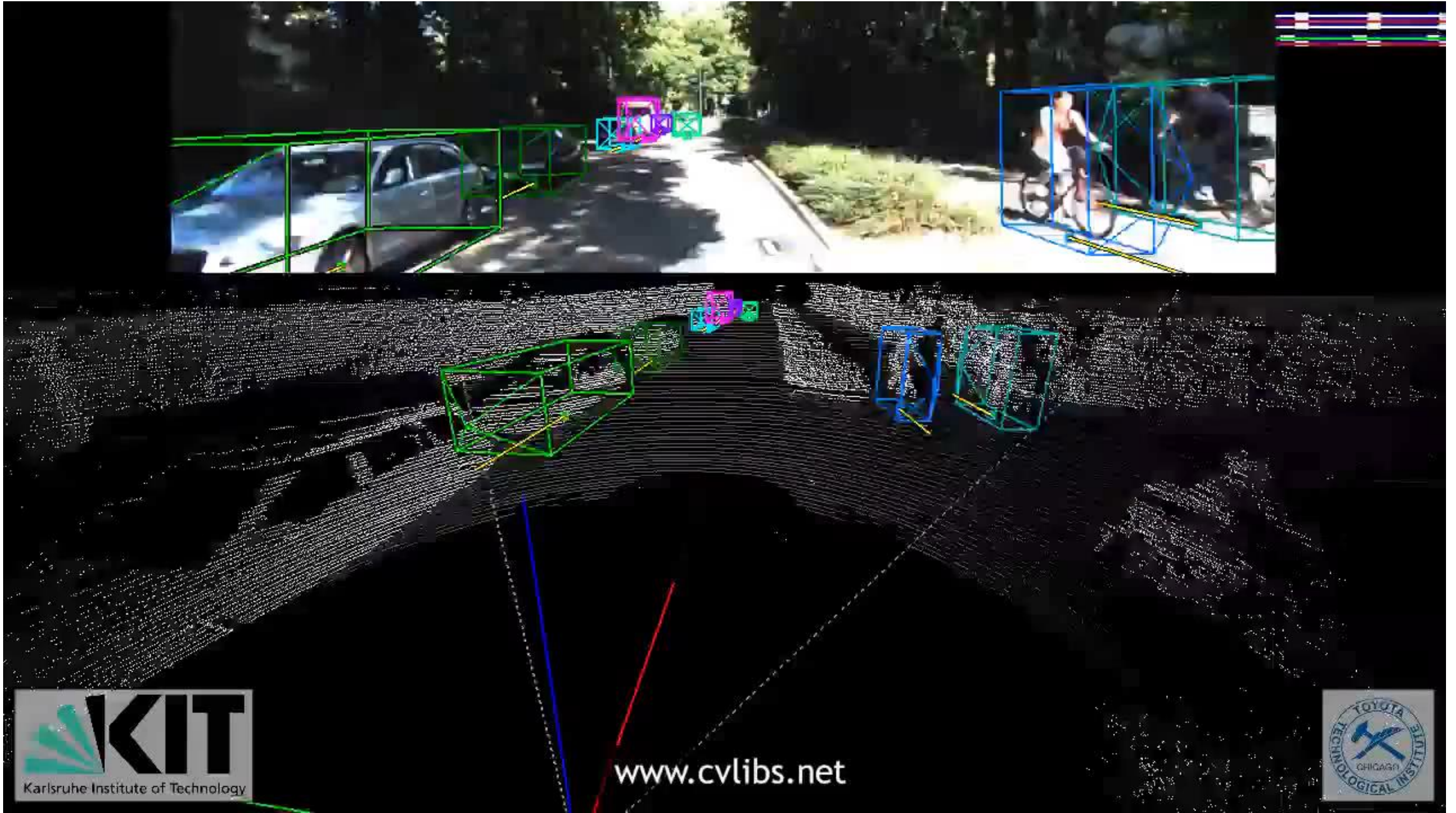
# Robot Autonomy

- Robot autonomy is a research area relying on tools from:
  - **Computer Vision & Signal Processing:** to deal with real-world signals in real time (e.g., filtering sound, convolving images, recognizing objects)
  - **Probability Theory & Estimation Theory:** to deal with uncertainty caused by sensor and actuator noise, computation and communication delays, and environment changes and estimate robot and world states
  - **Optimization Theory:** to plan the best robot behavior according to a suitable performance criterion
  - **Control Theory:** to execute the planned robot actions
  - **Machine Learning:** to improve the models and performance based on previous data (supervised, self-supervised, unsupervised, and reinforcement learning)

# Robot Autonomy



**Interaction with the real world introduces uncertainty!**

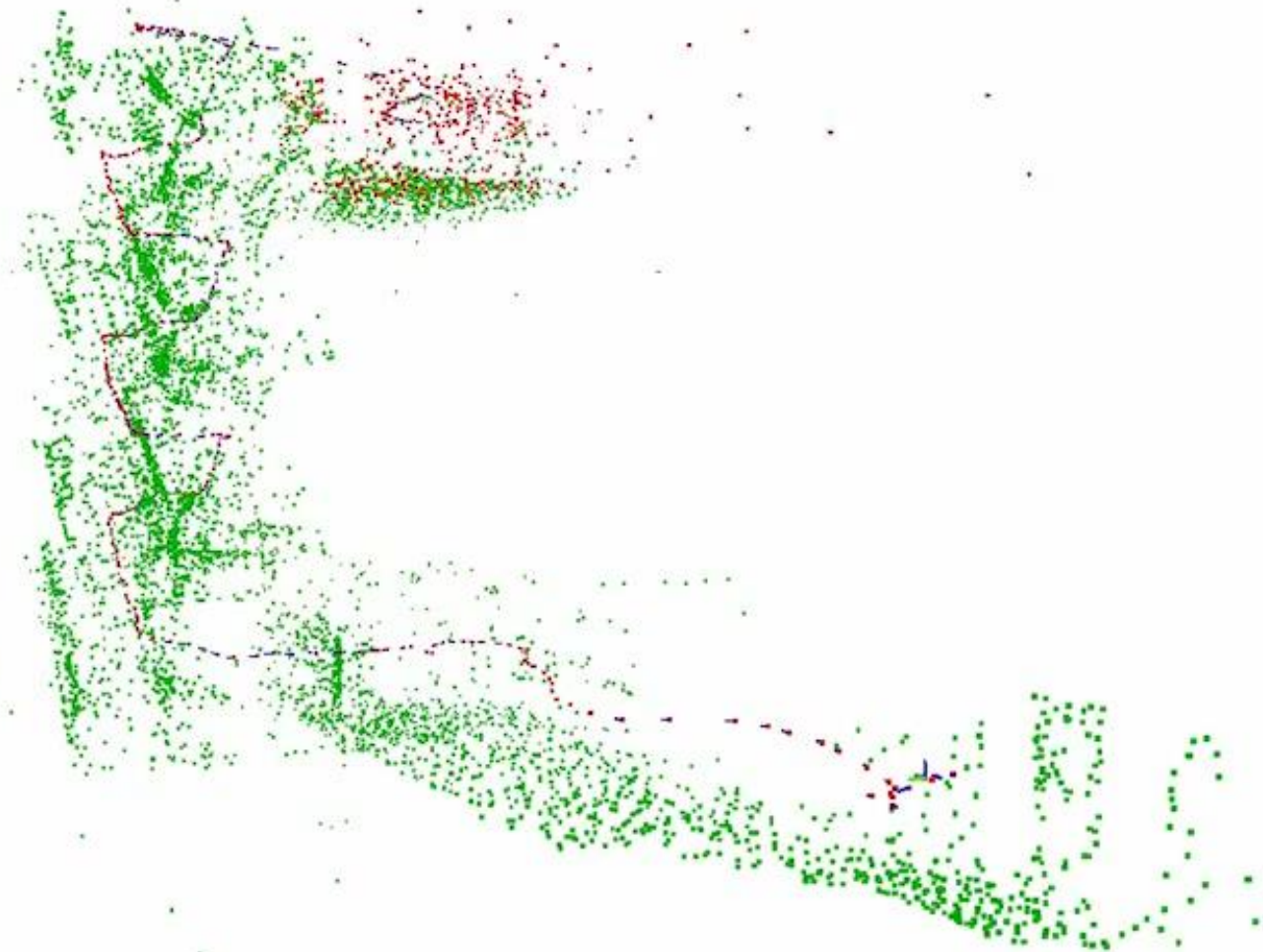




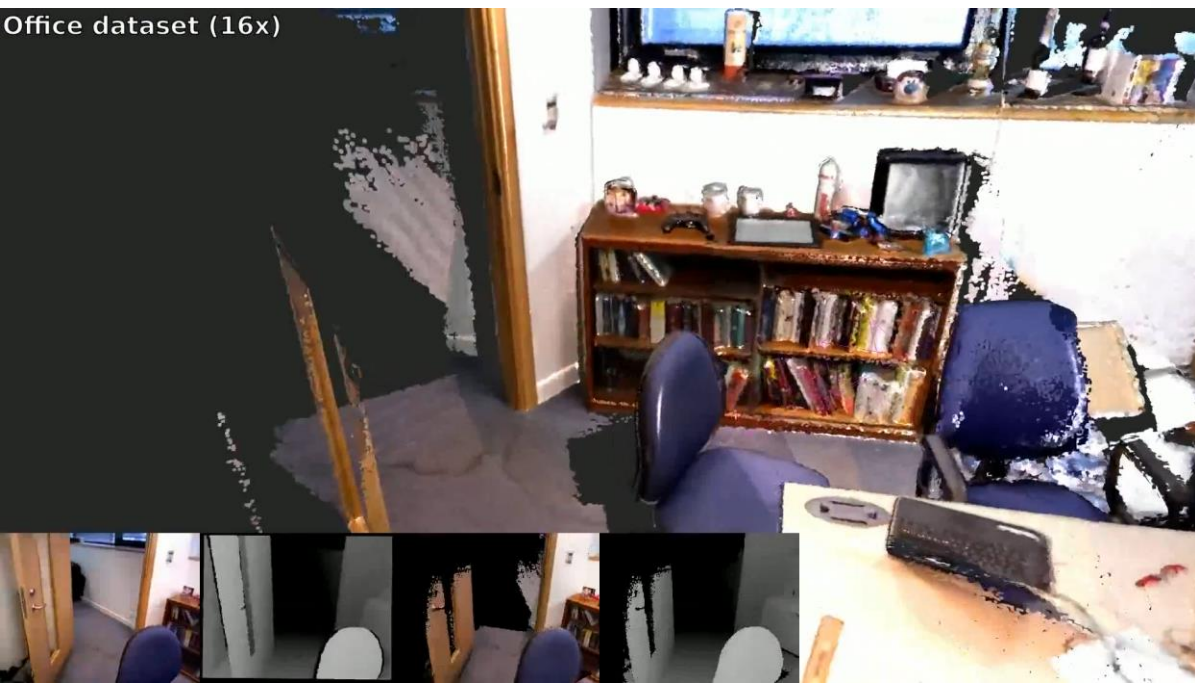


ESTIMATE

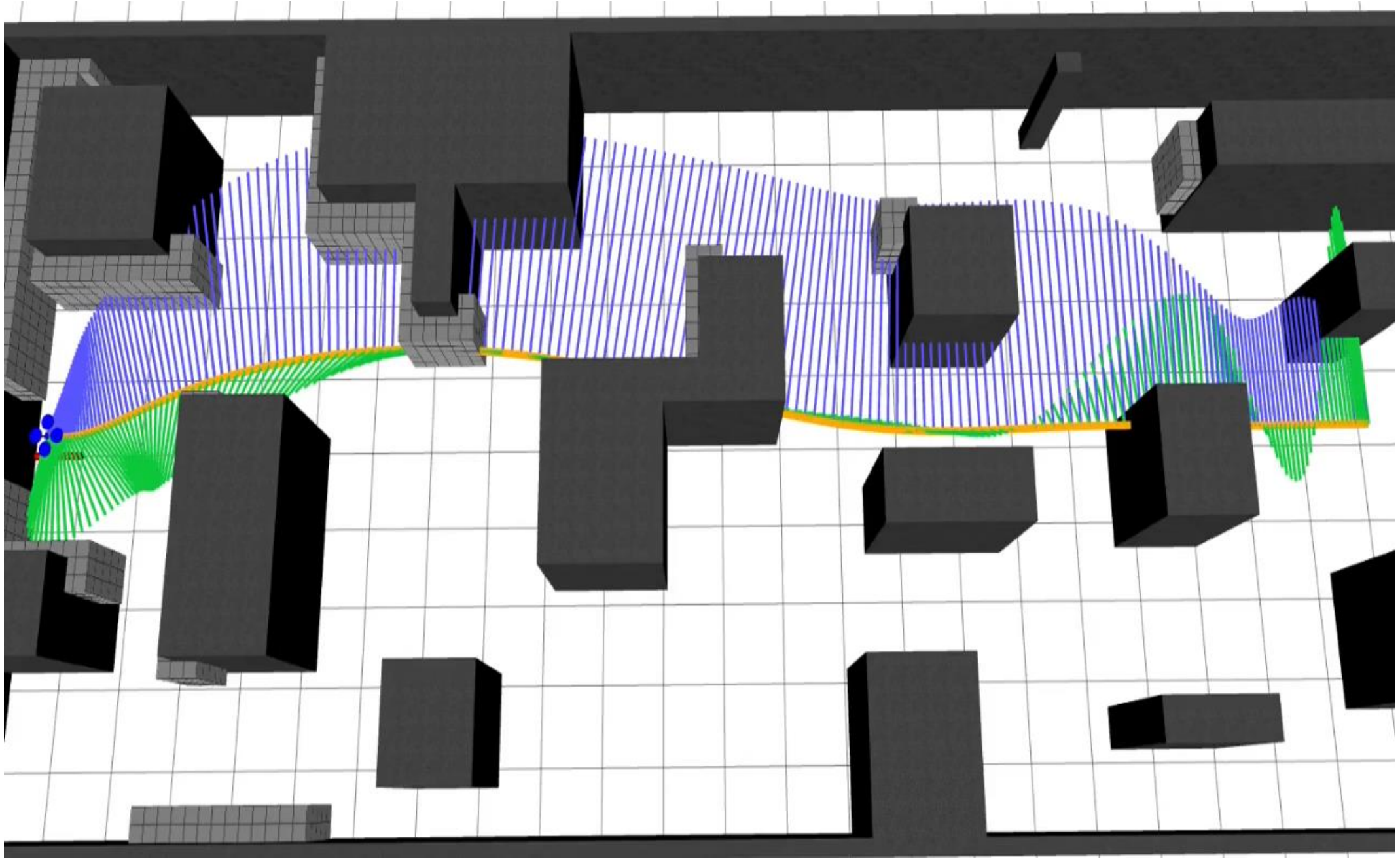
Forster, Carlone, Dellaert,  
Scaramuzza, RSS'15



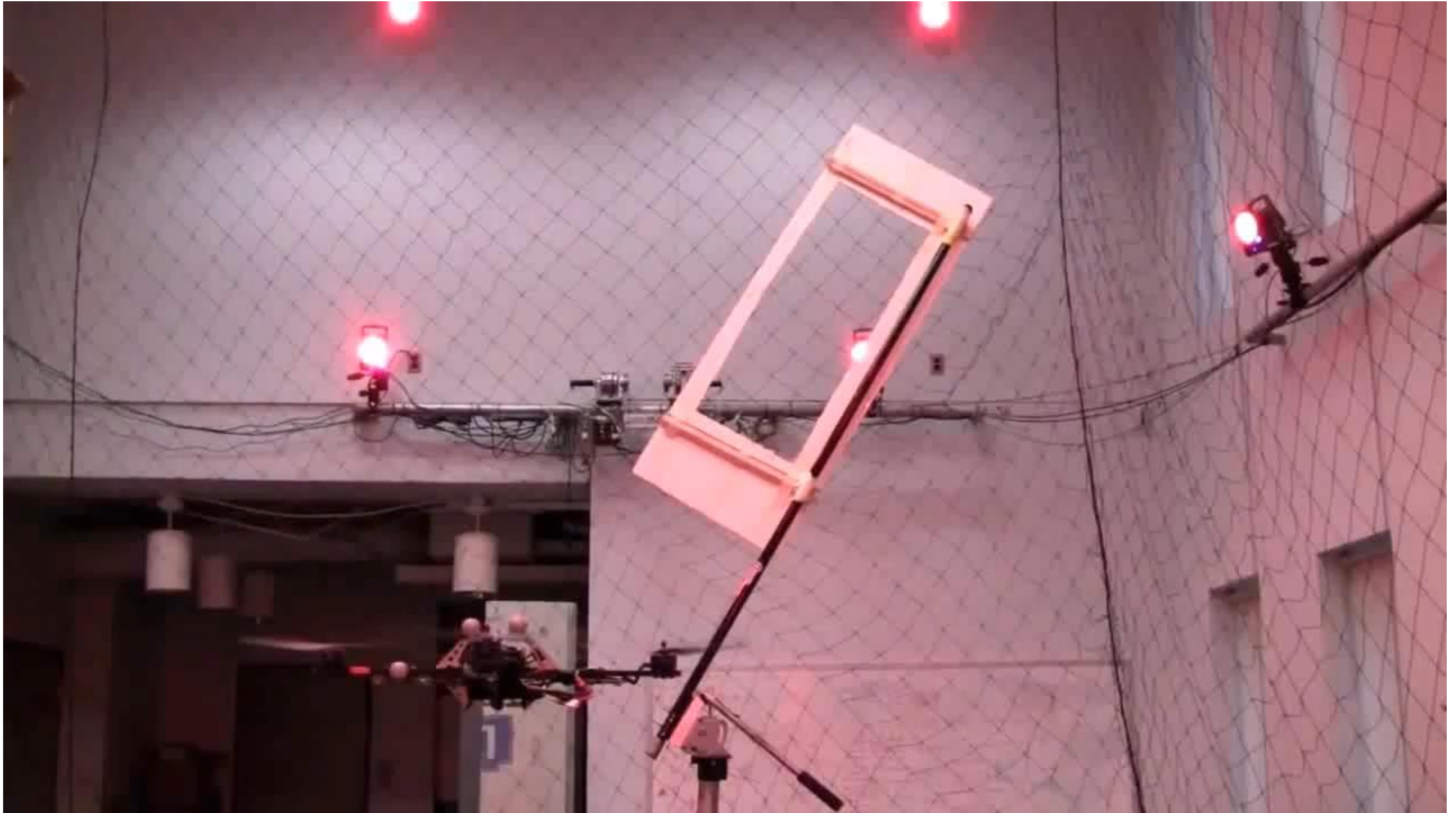
Office dataset (16x)



Whelan, Leutenegger, Salas-  
Moreno, Glocker, Davison, RSS'15







# ECE 276A: Sensing & Estimation in Robotics

- The course will cover theoretical topics in:
  - **Sensing**: image formation, classification, projective geometry, rotations, features, optical flow
  - **Estimation**: maximum likelihood estimation, probabilistic models, Bayesian filtering, localization, mapping, hidden Markov models
- Course website: <https://natanaso.github.io/ece276a>
  - Schedule, reading materials, and assignments
  - Grades: **GradeScope** (**SIGN UP!**)
  - Discussion: **Piazza** (**SIGN UP!**)
  - TA sessions:
    - Mon, Wed, 6:20 pm – 7:00 pm (Nikolay)
    - Tue, 4:00 pm – 5:00 pm (Shan)
    - Fri, 11:00 am – 12:00 pm (Arash)
- References (not required, see course website):
  - State Estimation for Robotics: Barfoot (**main reference, available online**)
  - An Invitation to 3-D Vision: Ma, Kosecka, Soatto & Sastry
  - Probabilistic Robotics: Thrun, Burgard & Fox
  - Bayesian Filtering and Smoothing: Sarkka



# A Warning About Prerequisites

- This is a challenging graduate-level course
- As graduate students, **I expect you to be mature and carefully evaluate whether you are prepared to take the course**
- I want everyone to learn about robotics, so the prerequisites are not strictly enforced
- Prerequisites:
  - **Probability Theory**: if you have not had a good course on probability theory it is too early to take ECE276A
  - **Linear Algebra**: if you have not had a good course on linear algebra, it is too early to take ECE276A
  - **Programming experience**: if you have not done programming projects of reasonable complexity before, it is too early to take ECE276A
- You will enjoy this course and learn a lot more if you have the right background
- Every year some students ignore this, overestimate their background knowledge or available time and have an unpleasant experience

# Grading

- Assignments:
  - 3 theoretical homeworks (16% of the grade)
  - 3 programming assignments in **python** with project reports (18% of the grade each)
  - Final exam (30% of grade)
- There is sufficient time to complete every assignment if you start **early**
- Late submissions and deadline extensions **will not be possible** because our schedule is **very tight** (1 week background review, 3 weeks per project, final exam)
- Letter grades will be assigned based on the class performance, i.e., you do not need to (and will not be able to) get everything right in order to get a good grade
- Piazza is a great place for discussion, and I encourage you to use it
- Students like to ask many questions but rarely help others. I will give **extra credit** (e.g., assign A to someone on the cut-off between A- and A) to students who answer questions on Piazza.

# Collaboration and Academic Integrity

- An important element of academic integrity is fully and correctly acknowledging any materials taken from the work of others – provide references for papers and **acknowledge in writing people you discuss with**
- You are encouraged to discuss the assignments with other students in general terms but the **work you do and turn in should be completely your own**
- Every assignment in this course is individual
- **Cheating will not be tolerated**
- Instances of academic dishonesty will be penalized via grade reduction and may be referred to the Office of Student Conduct for adjudication



# Project Report: Suggested Structure

1. **Introduction:** brief discussion of what is the problem and why it is important

It is important to monitor the humidity of plants and choose optimal watering times. In this paper, we present an approach to select the best watering time in the week from given historical humidity data.

2. **Problem Formulation:** brief rigorous mathematical statement of the problem

*Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be the average historical weakly humidity.*

**Problem:** Find a watering time  $t^* \in \mathbb{R}$  such that  $t^* = \underset{t}{\operatorname{argmin}} f(t)$

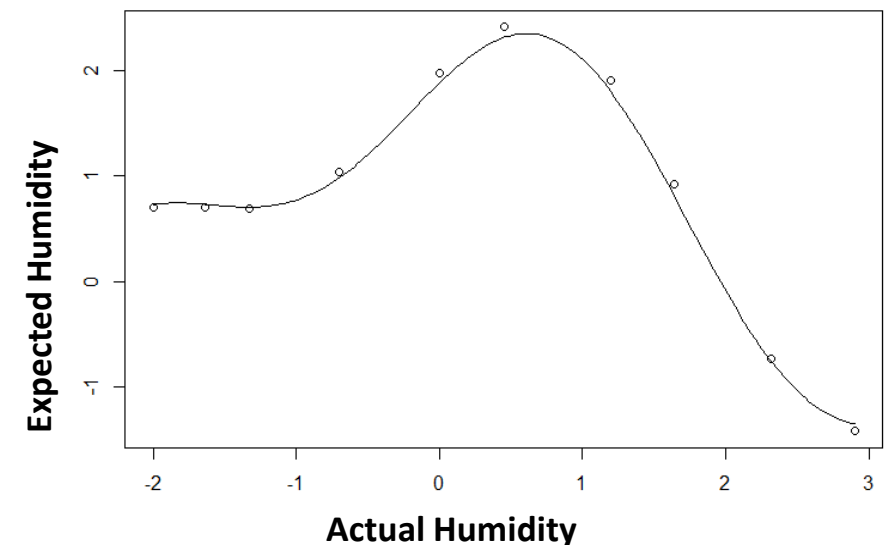
3. **Technical Approach:** description of the ideas, equations, algorithms used to solve the problem

The minimum of a function appears at one of its critical points

$\{s \in \mathbb{R} \mid f'(s) = 0\}$ . We find all the roots of  $f'$  and select the smallest one as the optimal watering time.

4. **Results:** figures showing qualitative and quantitative performance supported by discussion of what was successful and what fails

The method performs well as shown in Fig. 1. The performance could be improved if real-time humidity measurements are used to update  $f$ .



# Project Report: Examples

[https://natanaso.github.io/ref/Wang\\_LearningNavigation\\_SCR19.pdf](https://natanaso.github.io/ref/Wang_LearningNavigation_SCR19.pdf)

[https://natanaso.github.io/ref/Schlottfeldt\\_AdversarialInfoAcquisition\\_RSS18\\_Workshop.pdf](https://natanaso.github.io/ref/Schlottfeldt_AdversarialInfoAcquisition_RSS18_Workshop.pdf)

[https://natanaso.github.io/ref/Lauri\\_MonteCarloTreeSearch\\_ICRA15\\_Workshop.pdf](https://natanaso.github.io/ref/Lauri_MonteCarloTreeSearch_ICRA15_Workshop.pdf)

## Learning Navigation Costs from Demonstration via Differentiable Planning

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**Abstract**—This paper focuses on learning cost functions that capture desirable behavior in tasks demonstrated by an expert. In a task such as autonomous navigation in unknown environments, it is possible to obtain sequences of observations (e.g., images, states (e.g., poses), and control inputs but not direct queries of the underlying task-specific cost function. Hence, it is necessary to design a planning algorithm that, depending on the current cost representation, computes a control policy and propagates its error with respect to the demonstrations back to the cost representation. Our contribution is a probabilistic environment representation for local observation updates and cost function design, and a differentiable planning algorithm that performs state expansions only on a subset of promising states. Our complete model can be trained end-to-end and improves upon Value Iteration Networks and the Dyna-Q algorithm.

**Index Terms**—Inverse Reinforcement Learning, Differentiable Planning, Cost Learning

### I. INTRODUCTION

Autonomous robot systems increasingly require operation in unstructured, partially known, and dynamically changing environments. One core challenge for safe and robust navigation is that the *true* cost function of a navigation task, requiring safe, dynamically feasible, and efficient behavior, is generally not known while expert demonstrations can be utilized to uncover the underlying cost function [1], [2]. In addition, humans and animals can navigate successfully with partial knowledge of the environment and adapt when facing new obstacle configuration based on prior experience. Motivated by this observation, we focus on learning a cost function from demonstration that is not universally accurate over the state and control space but rather captures task-relevant information and leads to desirable behavior.

Our main contribution is an end-to-end differentiable model that combines a cost function representation and an efficient planning algorithm (see Fig. 1). The novelty of our approach is that the proposed model is fully differentiable, which allows using gradient-based optimization to improve the parameterized cost function. Our experiments show that the end-to-end differentiable model learns task-specific cost functions and improves upon Value Iteration Networks (VIN) [3] and the Dyna-Q algorithm [4] by handling partial and noisy observations. In summary, we offer the following contributions:

We gratefully acknowledge support from NSF CRII RI IIS-1755568.

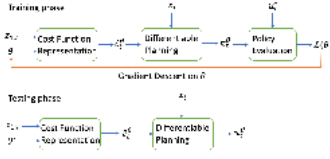


Fig. 1: Architecture for learning cost function representations from demonstrations via differentiable planning. During training, the goal is to learn a cost function parameterization  $\theta$  based on demonstrations, consisting of states  $x_{1:t}$ , controls  $u_{1:t}$ , and partial observations  $z_{1:t}$ , so that a control policy generated based on the learned cost incurs minimum loss  $\mathcal{L}(\theta)$ . Both the cost function representation  $\theta$  and the control policy  $\pi$  need to be differentiable with respect to  $\theta$  for error backpropagation. During testing in a new environment, online observations  $z_{1:t}$  and the trained parameters  $\theta^*$  provide the cost function necessary to generate a control policy.

- A cost function representation that incorporates a log-odds occupancy representation of the environment, updatable using a parameterized observation model.
- An efficient planning algorithm, which performs local convolutional operations encoding Bellman backups only on a subset of promising states. We guarantee that the output policy is differentiable with respect to the input cost function.
- An end-to-end differentiable model that learns task-specific cost functions from expert demonstrations by backpropagating policy performance loss through the planning algorithm and the cost representation.

### II. PROBLEM FORMULATION

Consider a robot navigating in an unknown environment with the task of reaching a goal state  $x_g \in \mathcal{X}$ . Let  $x_t \in \mathcal{X}$  be the discrete time robot state. For a given control input  $u_t \in \mathcal{U}$ , the robot state evolves according to known deterministic dynamics:  $x_{t+1} = f(x_t, u_t)$ . Let  $m^*$  be a function

## Adversarial Information Acquisition

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**Abstract**—This paper considers a non-cooperative two-player game modeling the problem of adversarial information acquisition in robotics. Each robot is equipped with a sensor, and is tasked with choosing control inputs that maximize an information (e.g., entropy) about the other player, while keeping its own state as uncertain to the other player as possible, subject to the available sensors. This adversarial information gathering problem has applications in surveillance, or search-and-rescue missions where the agent whose state is to be estimated may try to actively avoid the sensing robot. We formulate the problem of adversarial information acquisition, and provide an initial solution based on a variant of Monte Carlo Tree Search for simultaneous action games.

### I. INTRODUCTION

In this paper, we consider the problem of two robots interacting in an adversarial game where each robot attempts to estimate the state of its adversary, while keeping its own state hidden. This problem can have applications in search-and-rescue applications, where the agent to be found is mobile, and actively evades the sensing robot. In these problems, it is important to both accurately localize the target agent, while keeping one's own state hidden so that the target's ability to actively evade is reduced.

There is much prior work in the literature concerning the dynamics of pursuit-evasion in mobile robotic settings [3]. Approaches to the pursuit-evasion problem are split between considering the worst-case evader (adversary), and using probabilistic frameworks which consider the expected case. A common theme in the pursuit-evasion literature is the objective of reducing the distance to the evader to zero, or forcing the evader into a sensing footprint. In contrast, our problem is formulated using a probabilistic approach which optimizes an information theoretic quantity, namely entropy, about the distribution of the target to be tracked. Rather than closing distance to the target, our approach aims to produce the best estimate of the target's state, subject to the sensors available.

Our previous work considers the information acquisition problem for target tracking [1], however this work assumes that the target being tracked moves independently of the sensing robot, and crucially is not trying to actively evade the sensing robot. In this work, the problem formulation is symmetric in the sense that the adversary is trying to maximize information gained about us, and also minimize the information we can gain about it.

We also draw attention to some biological inspiration for this problem. Motion camouflage [9] is a strategy utilized by dragonflies, which enables them to capture their prey by minimizing the optical flow of their motion. Mischiati and Krishnaprasad [8] consider the problem of mutual motion camouflage, where two agents each pursue each other, but attempt to maintain a constant bearing to avoid detection by the other agent. Our problem is related, but rather than considering pursuit-evasion, we consider the dynamics of an *adversarial information gathering game*.

In the most general case, the information acquisition game proposed is a stochastic game and is difficult to solve. McEneaney [7] discusses a class of stochastic games with finite-dimensional solutions and dynamic programming algorithms to solve them. With some assumptions on the motion and observation models of the agents in our game, the problem can be simplified to a deterministic game. McEneaney [6] introduces a curse-of-dimensionality free max-plus method for deterministic game problems, which is likely to be very applicable to the linear Gaussian version of the information-theoretic game introduced here. Additionally, Grinwald and Dawid [4] present a game-theoretic argument that maximizing entropy and minimizing worst-case expected loss are duals of each other. A comprehensive treatment on adversarial reasoning, is provided in the book by Kott and McEneaney [5]. The approach taken in this work is a variant of Monte Carlo Tree Search [11], for simultaneous action games. We present the details of this approach in Sec. III.

### II. PROBLEM FORMULATION

Consider a two-player partial information game with simultaneous moves. Each player  $i \in \{1, 2\}$  has a state  $x_{i,t}$  that evolves according to the following motion model:

$$x_{i,t+1} = f_i(x_{i,t}, u_{i,t}, w_{i,t}) \quad (1)$$

where  $u_{i,t} \in \mathcal{U}_i$  is a finite space of admissible moves (control inputs) and  $w_{i,t}$  is a random variable specifying the motion noise. Player  $i$  can observe its own state  $x_{i,t}$  and chooses its moves with the objective of tracking the evolution of the state of the other player. Each player is equipped with a sensor used to collect information about the other player according to the following observation model:

$$z_{i,t} = h_i(x_{i,t}, x_{j,t}, v_{i,t}) \quad (2)$$

## Active Object Recognition via Monte Carlo Tree Search

Mikko Lauri, Nikolay Atanasov, George J. Pappas, and Risto Ritala

**Abstract**—This paper considers object recognition with a camera, whose viewpoint can be controlled in order to improve the recognition results. The goal is to choose a multi-view camera trajectory in order to minimize the probability of having misclassified objects and incorrect orientation estimates. Instead of using *offline* dynamic programming, the resulting stochastic optimal control problem is addressed via an *online* Monte Carlo tree search algorithm, which can handle various constraints and provides exceptional performance in large state spaces. A key insight is to use an active hypothesis testing policy to select camera viewpoints during the rollout stage of the tree search.

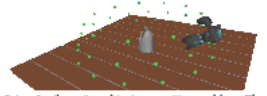


Fig. 1: Setup for the active object recognition problem. The camera position is restricted to a set of viewpoints (green) on a sphere centered at the object's location. The task is to choose a camera control policy, which minimizes the movement cost and the probability of misclassification.

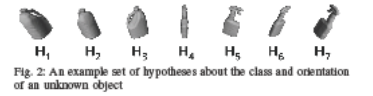


Fig. 2: An example set of hypotheses about the class and orientation of an unknown object

### I. INTRODUCTION

The goal of this paper is to choose a sequence of views for an RGB-D camera in order to identify the class and orientation of an object of interest (see Fig. 1). Unlike many existing approaches, which consider a next-best-view problem [1], [2], [3], we plan a multi-view camera trajectory to minimize the probability of having misclassified objects and incorrect orientation estimates. In previous work [4], we addressed a similar stochastic optimal control problem by casting it as a partially-observable Markov decision process. A point-based approximate solver [5] was used to obtain a non-greedy policy offline. Since repeated observations of the object from the same viewpoint provide redundant information, it is desirable to disallow viewpoint revisiting. The drawback of computing a policy offline is that revisiting and occlusion constraints are hard to incorporate and if the environment were to change, the computed policy would no longer be useful. The idea of this paper is to apply Monte Carlo tree search (MCTS, [6], [7]) to the active object recognition problem. MCTS is a variant of *online* planning approach which can handle various constraints and has exceptional performance in large challenging domains such as game solving [8], [9] and belief-space planning in robotics [10], [11], [12].

### II. PROBLEM FORMULATION

Let the camera pose at time  $t$  be  $x_t \in \mathcal{X} \subset SE(3)$ , where  $\mathcal{X}$  is a finite set of viewpoints on a sphere centered at the object's location (see Fig. 1). At time  $t$ , the camera can move to any of the viewpoints in  $\mathcal{X}$  and pays a cost  $g(x_{t-1}, x_t)$  which captures the energy expenditure. Let the true (unknown) class of the observed object be  $c \in \mathcal{C}$ . We formulate hypotheses about the class and orientation of the object:

$H(c, r)$ : the object class is  $c \in \mathcal{C}$  with orientation  $r \in \mathcal{R}(c)$ ,

$$\begin{aligned} \min_{\mu: \mathcal{C} \times \mathcal{R} \rightarrow \mathcal{X}} & \frac{1}{T} \sum_{t=1}^T g(x_{t-1}, x_t) + \lambda Pe(T) \\ \text{s.t. } & x_{t+1} = \mu_t(x_{0:t}, x_{0:t}) \quad t = 0, \dots, T-1, \\ & x_{t+1} \notin \{x_0, \dots, x_t\} \quad t = 0, \dots, T-1, \\ & x_t \sim q(\cdot | x_0, H_1) \quad t = 0, \dots, T, \\ & p_t = b(p_{t-1}, x_t, x_0) \quad t = 1, \dots, T, \end{aligned} \quad (1)$$

M. Lauri and R. Ritala are with the Department of Automation Science and Engineering, Tampere University of Technology, P.O. Box 692, FI-33101, Tampere, Finland, {mikko.lauri, risto.ritala}@utu.fi.  
N. Atanasov and G. Pappas are with GRASP Lab, University of Pennsylvania, Philadelphia, PA 19104, USA, {natanasov, pappasg}@seas.upenn.edu. This work was supported by Jernsheim, one of six centers of STARnet, a Semiconductor Research Corporation program sponsored by MARCO and DARPA.

<sup>1</sup>After a hypothesis is chosen, the discrete orientation estimate can be refined by aligning the observed object surface to the corresponding model in the training database, e.g., by using the iterative closest point algorithm.

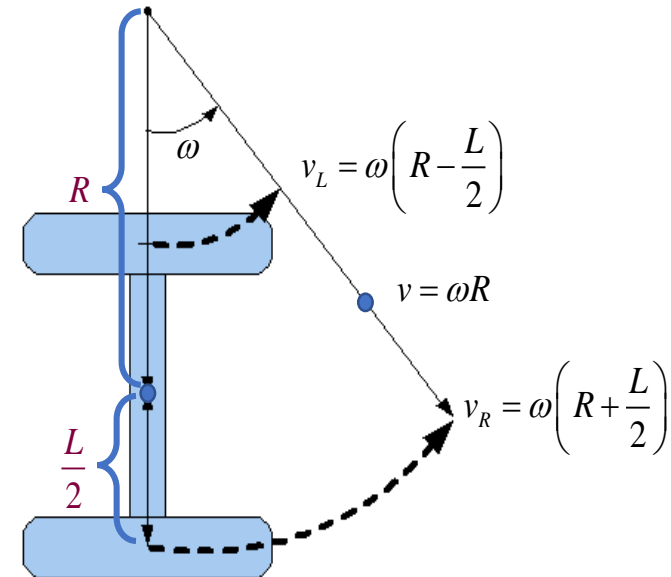
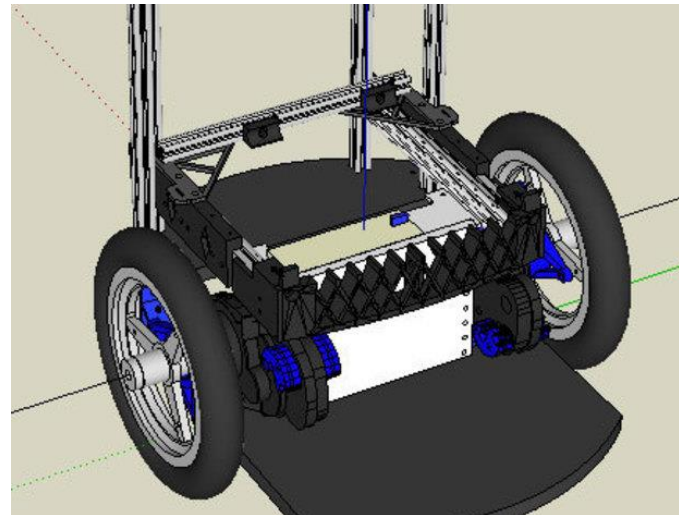
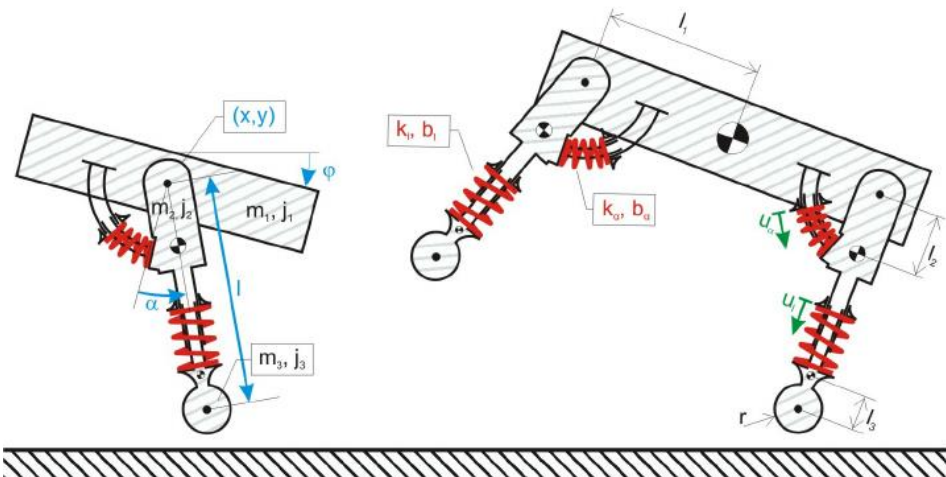
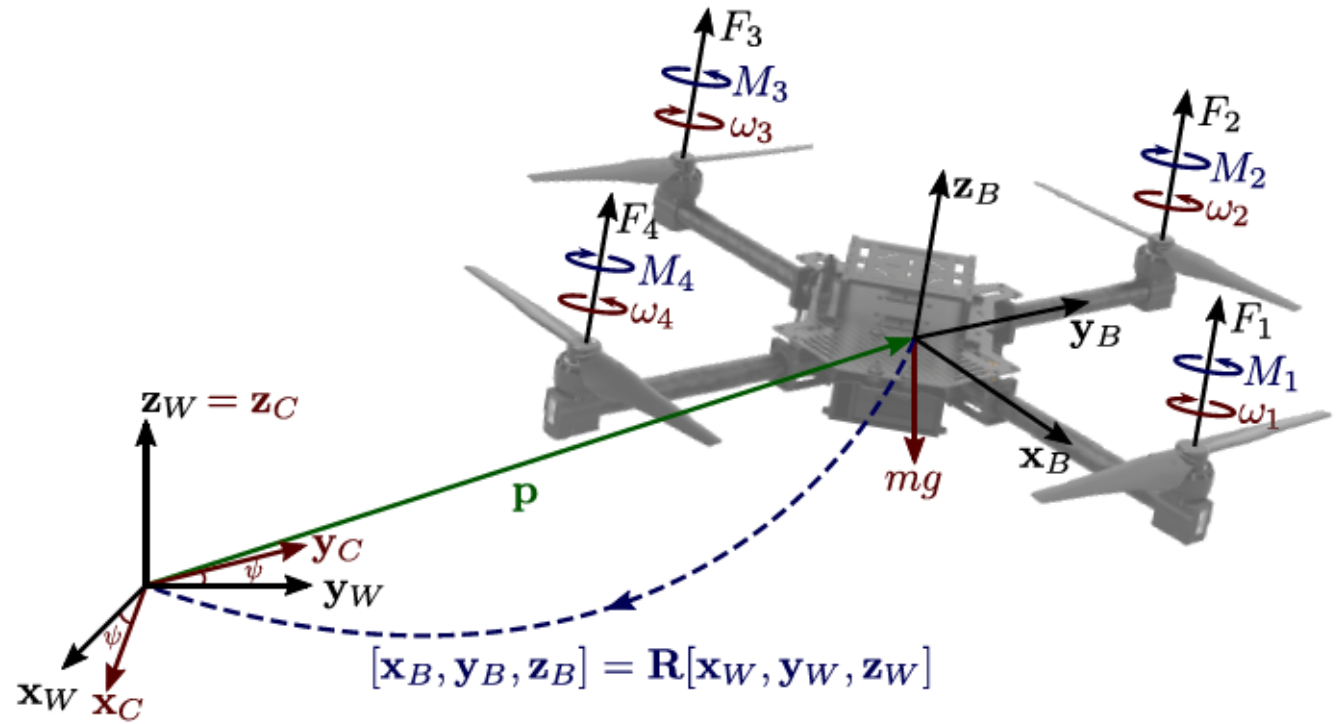
# Syllabus

Date	Lecture	Material	Assignment
Jan 04	Introduction		
Jan 06	Probability Theory Review	Barfoot-Ch.2	
Jan 11	Unconstrained Optimization	Barfoot-Ch.4.3.1, Matrix-calculus	HW1
Jan 13	Gaussian Discriminant Analysis	Mitchell-NaiveBayesLogReg	PR1
Jan 18	Martin Luther King Day (No class, Expectation Maximization)	Tomasi-EM	
Jan 20	Logistic Regression	Mitchell-NaiveBayesLogReg	
Jan 25	Rotations	Barfoot-Ch.6.1-6.3	
Jan 27	Motion and Observation Models	Barfoot-Ch.6.4	
Feb 01	Bayes Filter, Particle Filter	Barfoot-Ch.4.2	HW2
Feb 03	Catch up		PR2
Feb 08	Particle Filter SLAM	Thrun-Burgard-Fox-Ch.7-9	
Feb 10	Kalman Filter	Barfoot-Ch.3.3	
Feb 15	President's Day (No class, TBD)		
Feb 17	EKF, UKF	Barfoot-Ch.4.2	
Feb 22	SO(3) and SE(3) Groups	Barfoot-Ch.7.1-7.2	HW3
Feb 24	SO(3) and SE(3) Groups	Barfoot-Ch.7.1-7.2	PR3
Mar 01	Visual-Inertial SLAM		
Mar 03	Visual Features, Optical Flow	Image-Features	
Mar 08	Localization and Odometry from Point Features		
Mar 10	TBD		
Mar 15	Final Exam		



# Motion Models

- Based on **kinematics or dynamics**:
  - differential drive (roomba)
  - Ackermann drive (car, bicycle)
  - quadrotor, quadruped, humanoid, etc.
- Based on **odometry**:
  - use sensors to estimate change in the robot state over time
  - only available in retrospect
  - useful for localization and mapping but cannot be used for planning and control



# Observation Models

- **Position Sensor:** directly measures position (e.g., GPS, laser scanner, IR sensor, RGBD camera)
- **Velocity/Acceleration/Force Sensor:** measures linear acceleration or angular velocity or pressure or force (accelerometer, gyroscope, inertial measurement unit (IMU), tactile sensor)
- **Bearing Sensor:** measures angles (e.g., magnetometer, camera, microphone)
- **Range Sensor:** measures distances (e.g., radio)



FLIR RGB Camera



VectorNav IMU



Ublox GPS  
and Compass



Beaglebone  
Radio



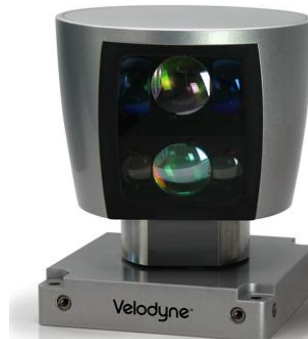
Intel RealSense  
RGBD Camera



Garmin Single-beam Lidar



Hokuyo  
2D Lidar



HDL-64E



HDL-32E

Velodyne  
3D Lidar



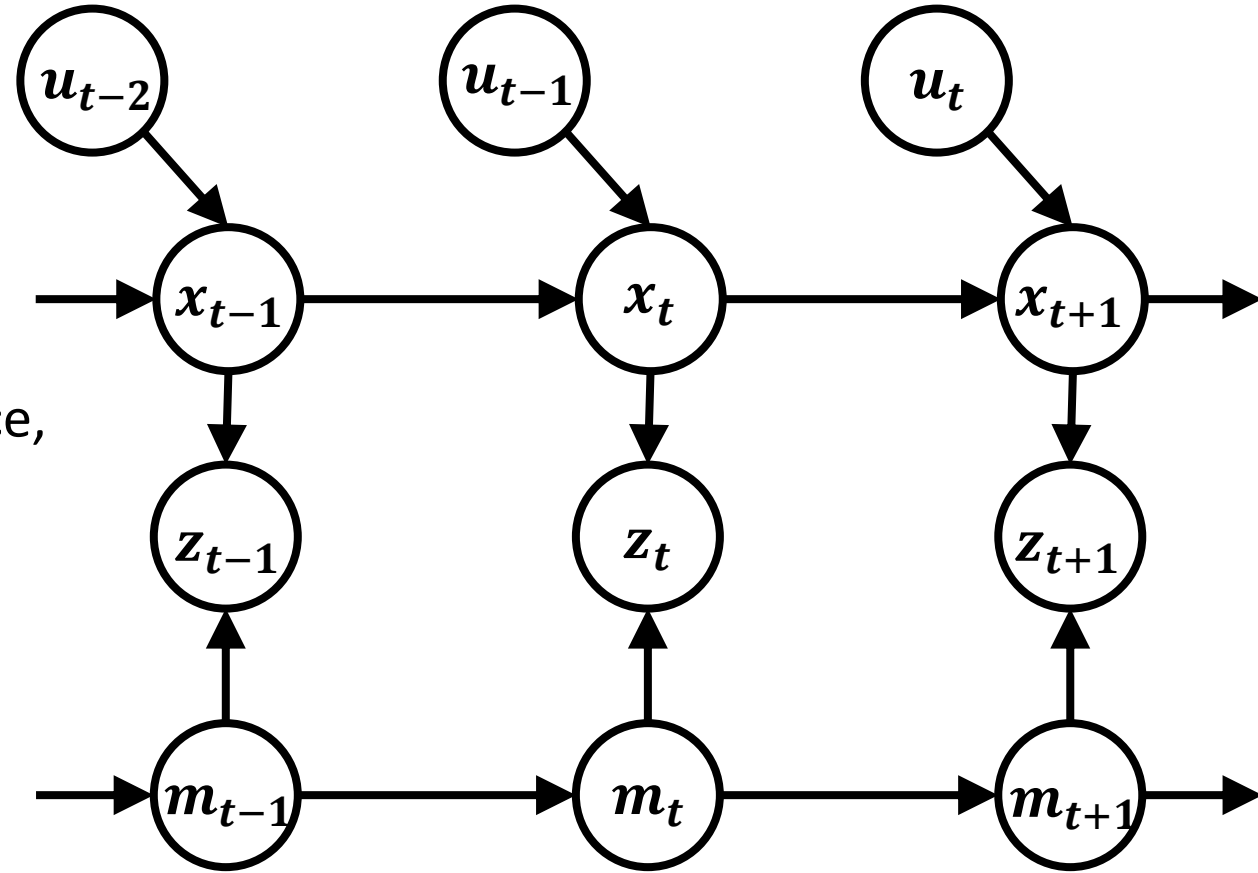
VLP-16



Hex 6-Axis  
Force/Torque  
Sensor

# Structure of Robotics Problems

- **Time:**  $t$  (discrete or continuous)
- **Robot state:**  $x_t$  (e.g., position, orientation, velocity)
- **Environment state:**  $m_t$  (e.g., map of free space, locations of objects)
- **Control input:**  $u_t$  (e.g., quadrotor thrust and moment of rotation)
- **Observation:**  $z_t$  (e.g., image, laser scan, radio signal, inertial measurements)
- **Motion Model:**  $p(x_{t+1}|x_t, u_t)$  --- describes the motion of the robot to a new state  $x_{t+1}$  after applying control input  $u_t$  at state  $x_t$
- **Observation Model:**  $p(z_t|x_t, m_t)$  --- describes the observation  $z_t$  of the robot depending on its state  $x_t$  and the map  $m_t$  of the environment





# Project 1: Color Classification

- Pixel-level color classification and shape-based object detection



```
66     if window.shape[0] != p.shape[0] or window.shape[1] != p.shape[1]:
67         continue
68
69     tempSim = compareImages(p, window)
70     if(tempSim > maxSim):
71         maxSim = tempSim
72         maxBox = (x, y, p.shape[0], p.shape[1])
73
74     t1 = time.time()
75
76     print("Execution time: " + str(t1 - t0))
77     print(maxSim)
78     print(maxBox)
```

detectStopSigns.py 64:43

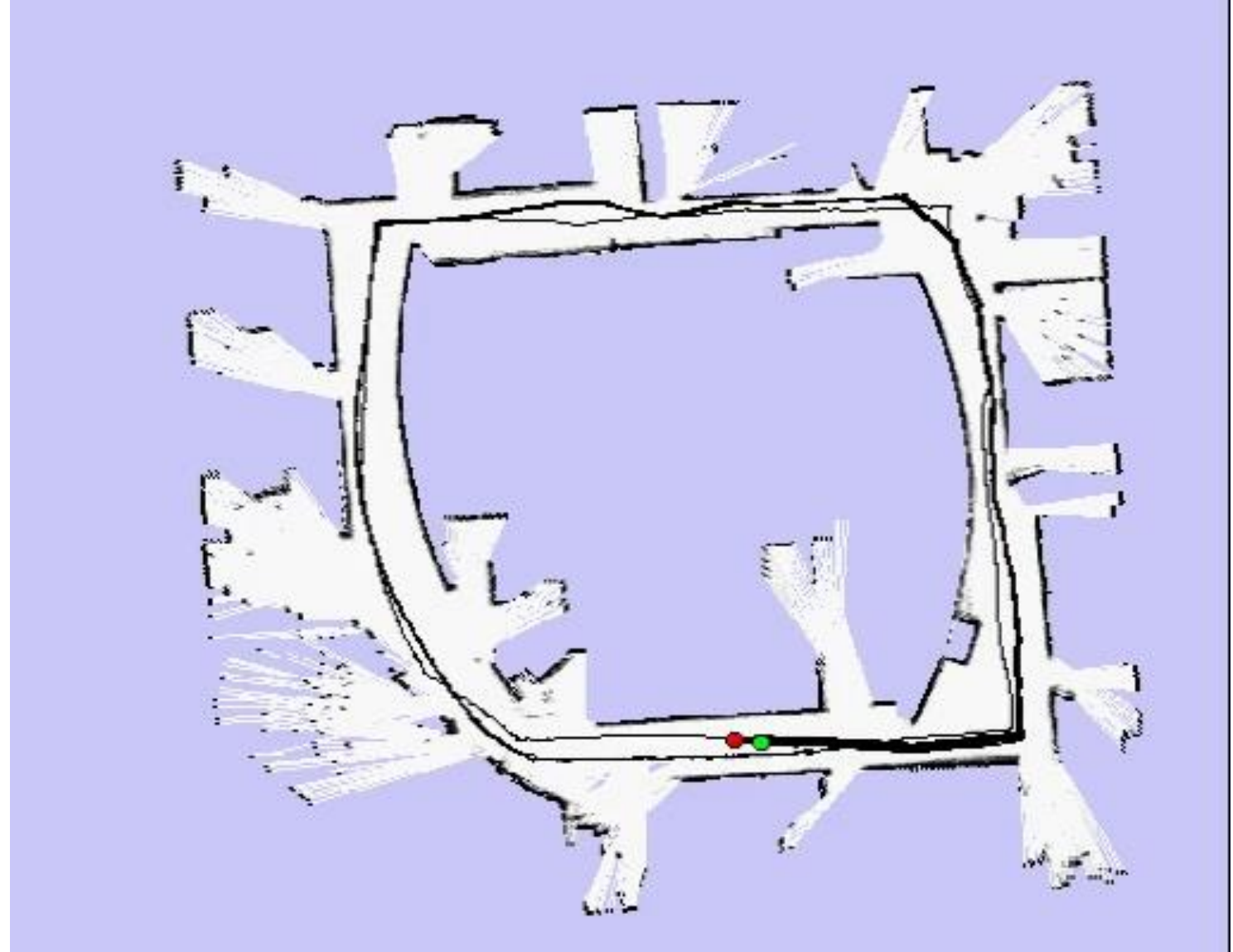
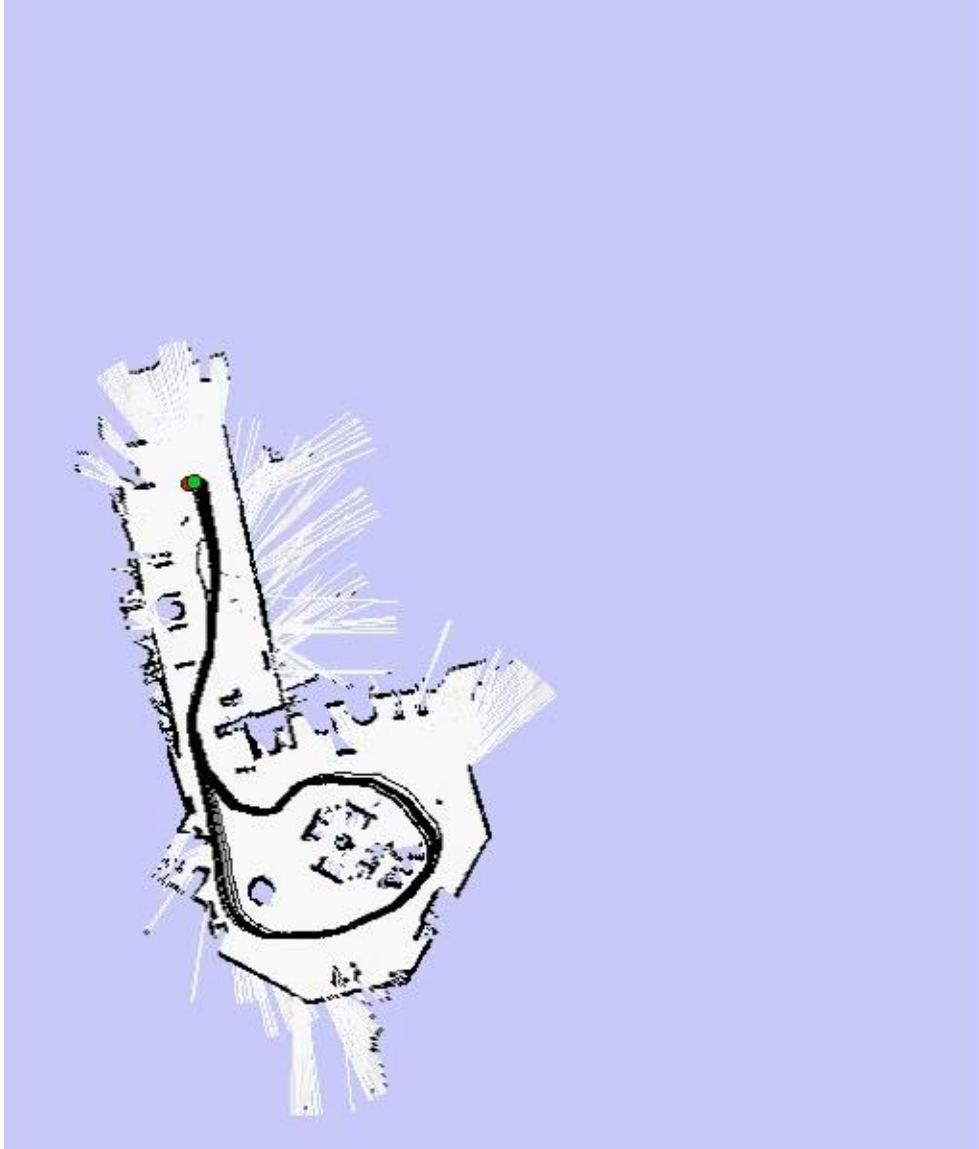
LF UTF-8 Python

Data from Michael Basilyan,  
<https://github.com/mbasilyan/Stop-Sign-Detection>

## Project 2: Particle Filter SLAM

Montemerlo et al., FastSLAM, AAAI'02

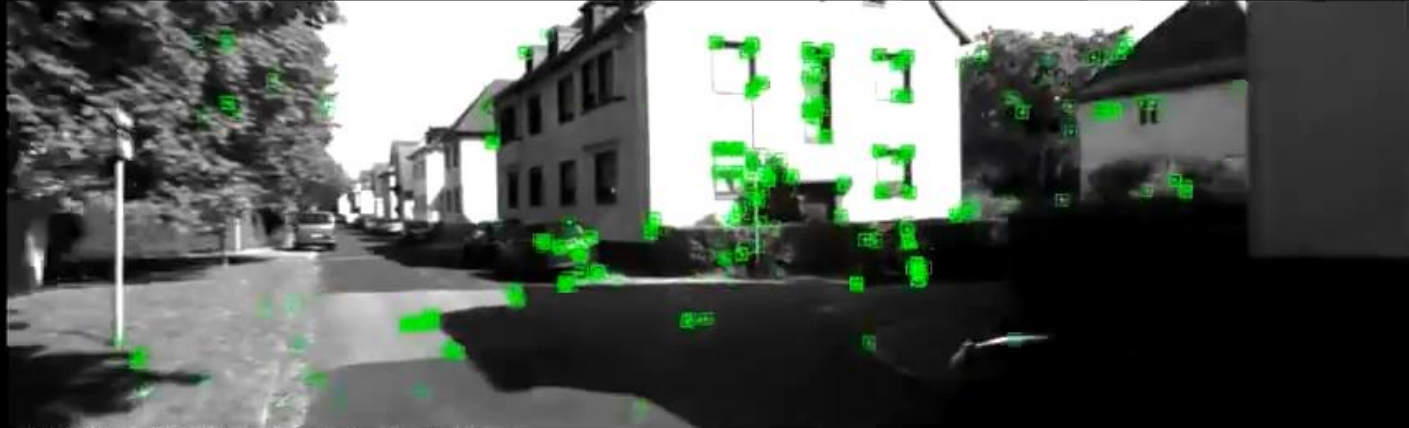
- Simultaneous localization and mapping (SLAM) using a lidar scanner



## Project 3: Visual Inertial SLAM

Mur-Artal et al., OrbSLAM, IEEE T-RO'15

- Kalman filter tracking of the 3-D pose of a moving body based on IMU and camera measurements



TRACKING — KFs: 456 , MPs: 34546 , Tracked: 353

