

# ECE276A: Sensing & Estimation in Robotics

## Lecture 1: Introduction

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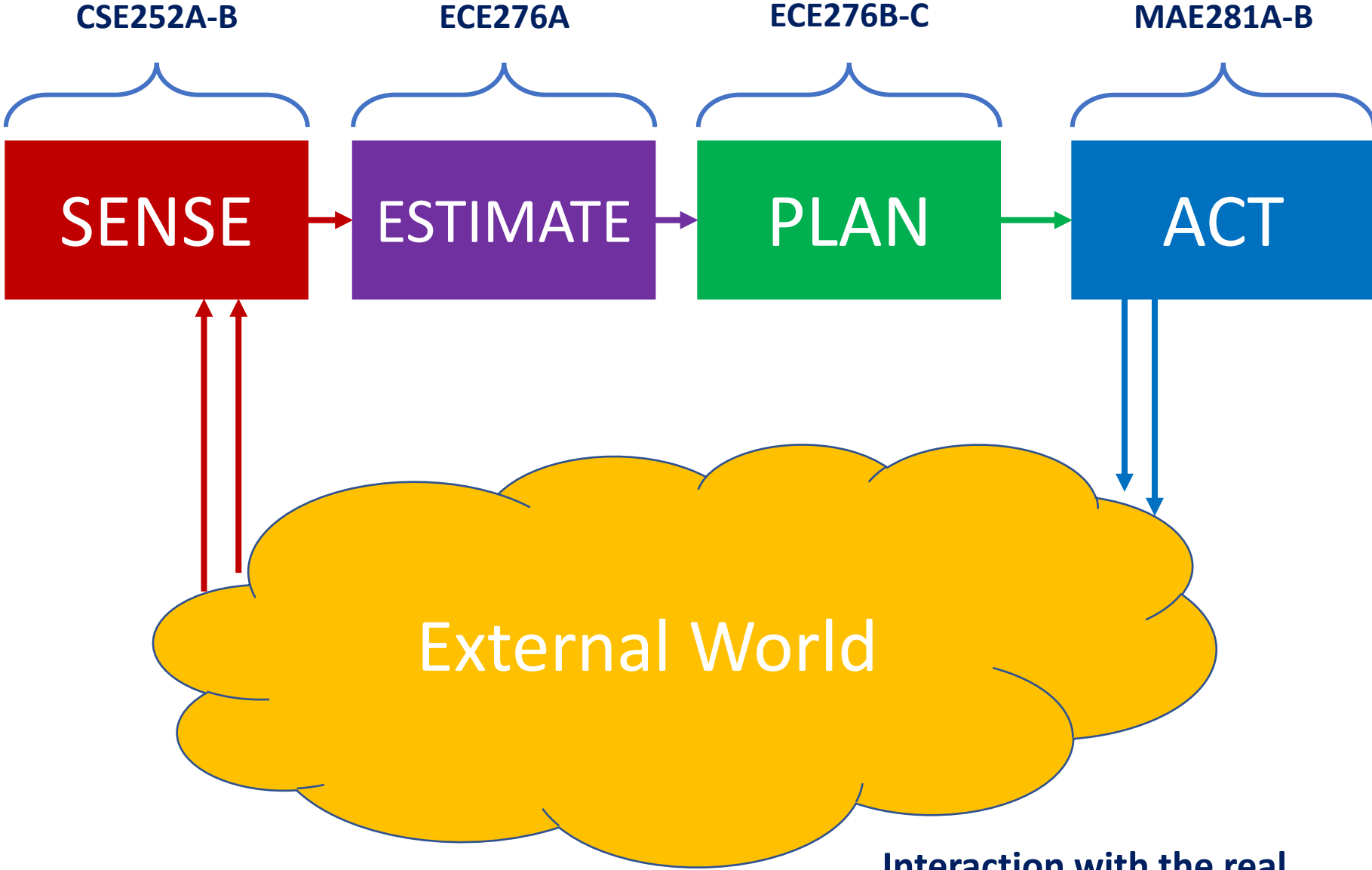
**UC San Diego**

**JACOBS SCHOOL OF ENGINEERING**  
Electrical and Computer Engineering

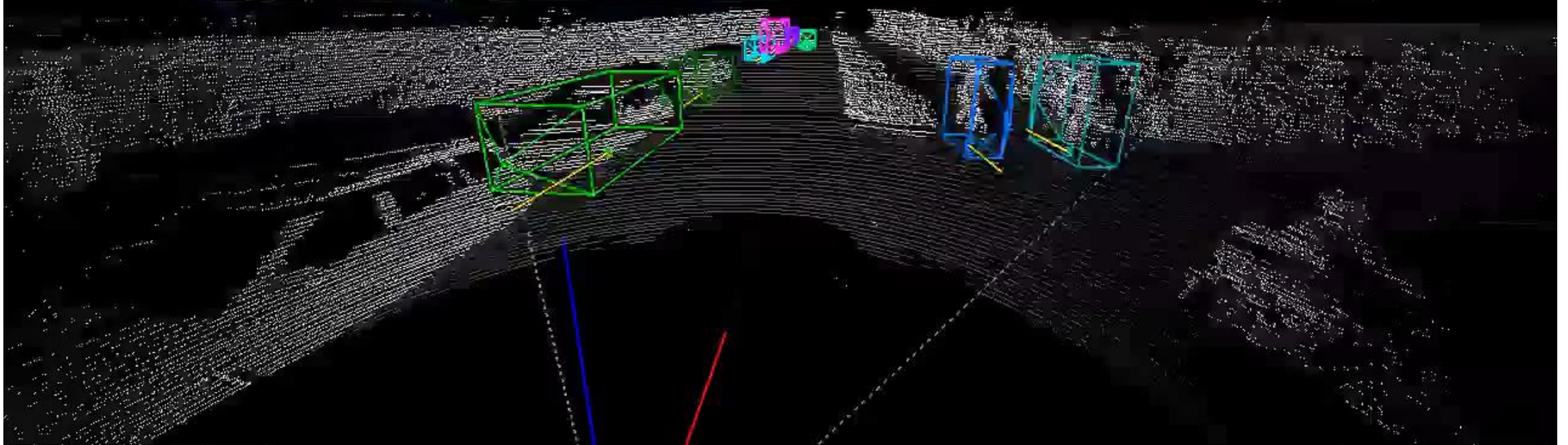
# Mobile Robot Autonomy

- Mobile robot autonomy is a research area relying on tools from:
  - **Computer Vision & Signal Processing:** to deal with real-world signals in real time (e.g., filtering sound, convolving images, recognizing objects)
  - **Probability Theory & Estimation Theory:** to deal with uncertainty caused by sensor and actuator noise, computation and communication delays, and environment changes and estimate robot and world states
  - **Optimization Theory:** to plan the best robot behavior according to a suitable performance criterion
  - **Control Theory:** to execute the planned robot actions
  - **Machine Learning:** to improve the models and performance based on data (supervised, self-supervised, unsupervised, and reinforcement learning)

# Robot Autonomy



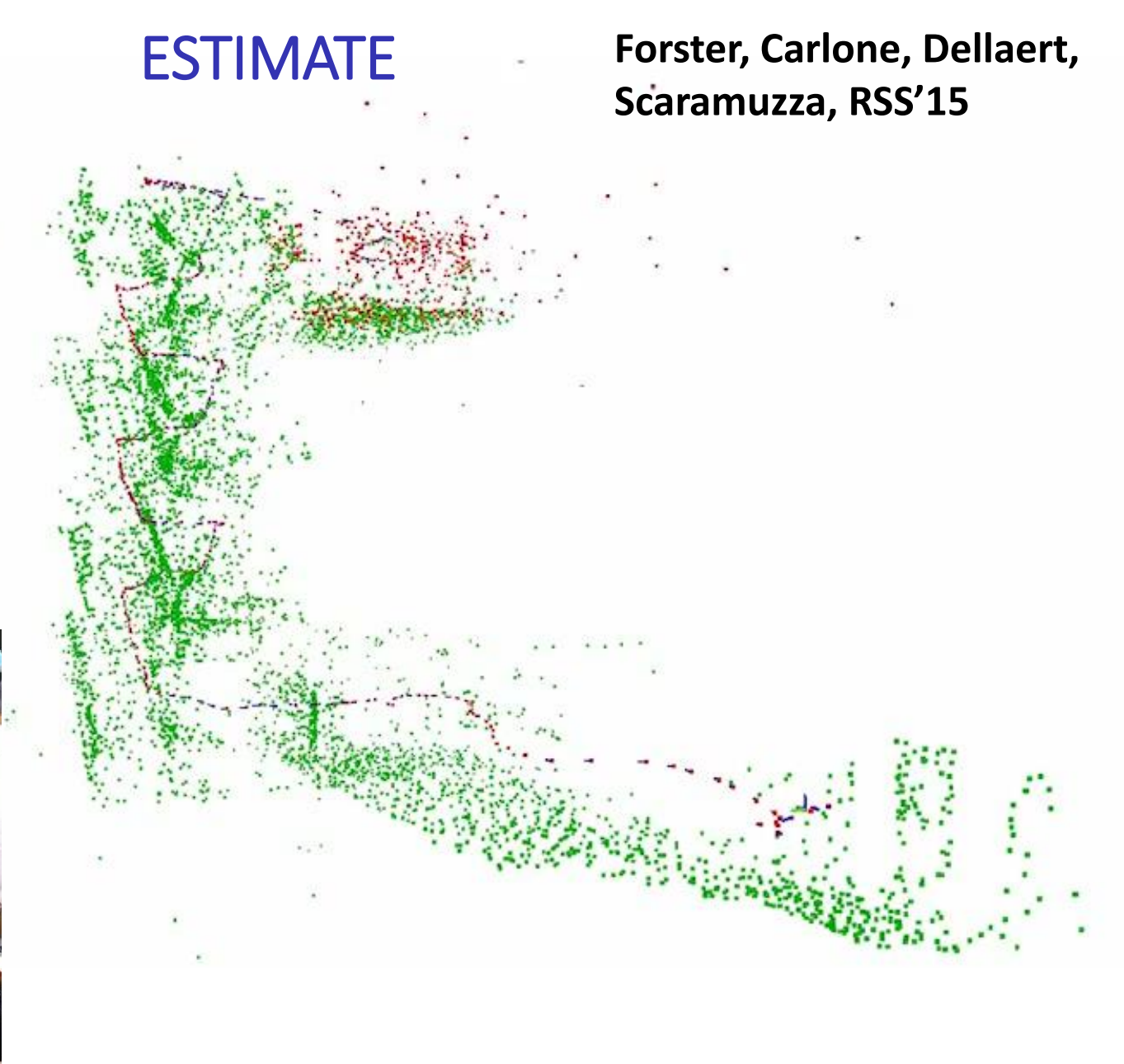
**Interaction with the real world introduces uncertainty!**



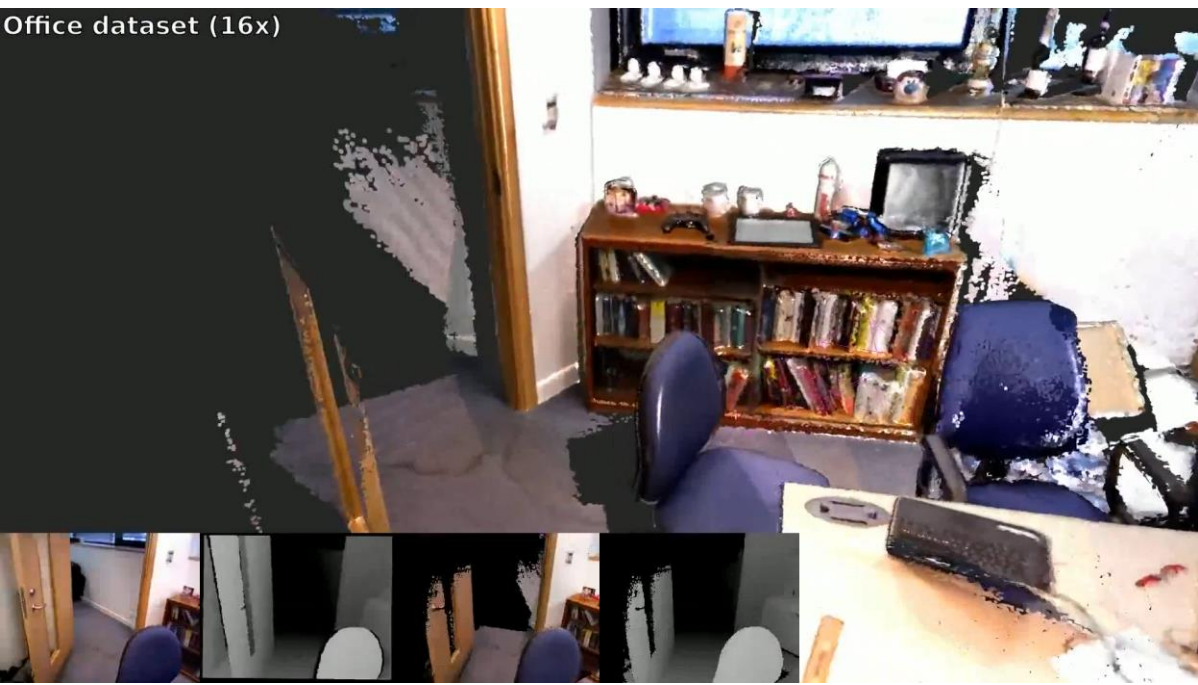


ESTIMATE

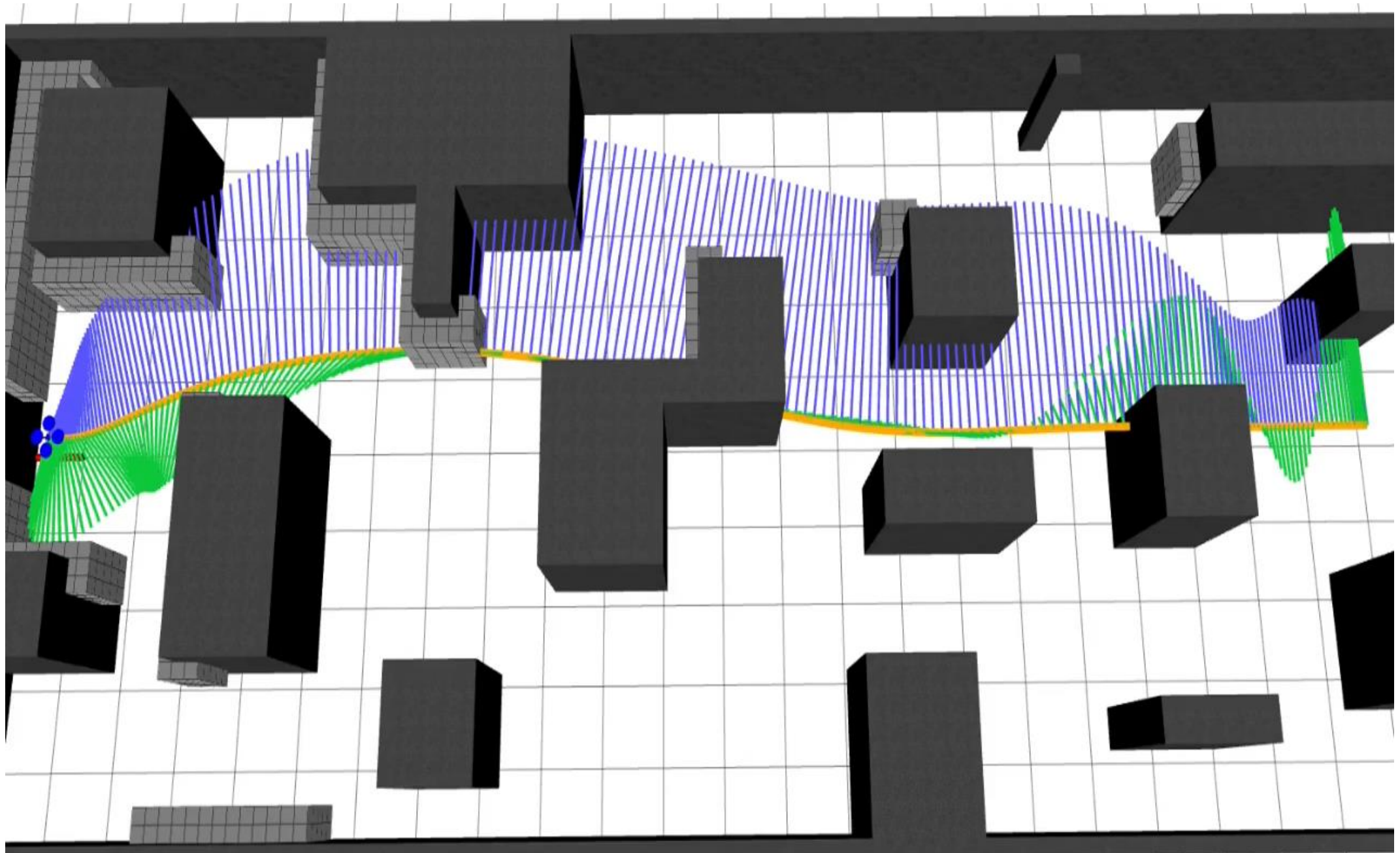
Forster, Carlone, Dellaert,  
Scaramuzza, RSS'15



Office dataset (16x)



Whelan, Leutenegger, Salas-Moreno,  
Glocker, Davison, RSS'15





# ECE 276A: Sensing & Estimation in Robotics

- The course will cover:
  - **Sensing:** image formation, projective geometry, rotations, features, optical flow
  - **Estimation:** probabilistic models, maximum likelihood estimation (MLE), Bayesian estimation, simultaneous localization and mapping (SLAM), hidden Markov models
- Course website: <https://natanaso.github.io/ece276a>
  - Schedule, reading materials, and assignments
  - Grades: **GradeScope (SIGN UP!)**
  - Discussion: **Piazza (SIGN UP!)**
  - Office hours/TA sessions: TBD
- References (**optional**):
  - State Estimation for Robotics: Barfoot
  - Probabilistic Robotics: Thrun, Burgard & Fox
  - An Invitation to 3-D Vision: Ma, Kosecka, Soatto & Sastry
  - Bayesian Filtering and Smoothing: Sarkka



# A Warning About Prerequisites

- This is a challenging graduate course
- I want everyone to learn about robotics, so the prerequisites are not strictly enforced
- As graduate students, **I expect you to be mature and carefully evaluate whether you are prepared to take the course**
- Prerequisites:
  - **Probability Theory:** if you have not had a good course on probability theory it is too early to take ECE276A
  - **Linear Algebra:** if you have not had a good course on linear algebra, it is too early to take ECE276A
  - **Programming experience:** if you have not done programming projects of reasonable complexity before, it is too early to take ECE276A
- You will enjoy this course and learn a lot more if you have the right background
- Every year some students ignore this, overestimate their prior preparation or available time and have an unpleasant experience

# Grading

- Assignments:
  - 3 theoretical homework assignments (16% of the grade total)
  - 3 programming assignments in **python** with project reports (18% of the grade each)
  - Final exam (30% of the grade)
- There is sufficient time to complete every assignment if you start **early**
- Late submissions and **deadline extensions will not be possible** because our schedule is **tight** (1 week background review, 3 weeks per project, final exam)
- Letter grades will be assigned based on the class performance, i.e., you do not need to and will not be able to get everything right in order to get a good grade
- Piazza is a great place for discussion, and I encourage you to use it
- In addition to asking questions, responding to others on Piazza is a great way to strengthen your knowledge

# Collaboration and Academic Integrity

- Every assignment in this course is **individual**
- You are encouraged to discuss the assignments with other students in general terms but the **work you do and turn in should be completely your own**
- An important element of academic integrity is fully and correctly acknowledging any materials taken from the work of others – provide references for papers and **acknowledge in writing people you discuss the assignments with**
- **Cheating will not be tolerated**
- Instances of academic dishonesty will be penalized via grade reduction and may be referred to the Office of Student Conduct for adjudication

# Project Report: Suggested Structure

1. **Introduction:** brief discussion of what the problem is and why it is important

It is important to monitor the humidity of plants and choose optimal watering times. In this paper, we present an approach to select the best watering time in the week from given historical humidity data.

2. **Problem Formulation:** brief rigorous mathematical statement of the problem, not the solution!

*Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be the average historical weakly humidity.*

**Problem:** Find a watering time  $t^* \in \mathbb{R}$  such that  $t^* = \underset{t}{\operatorname{argmin}} f(t)$

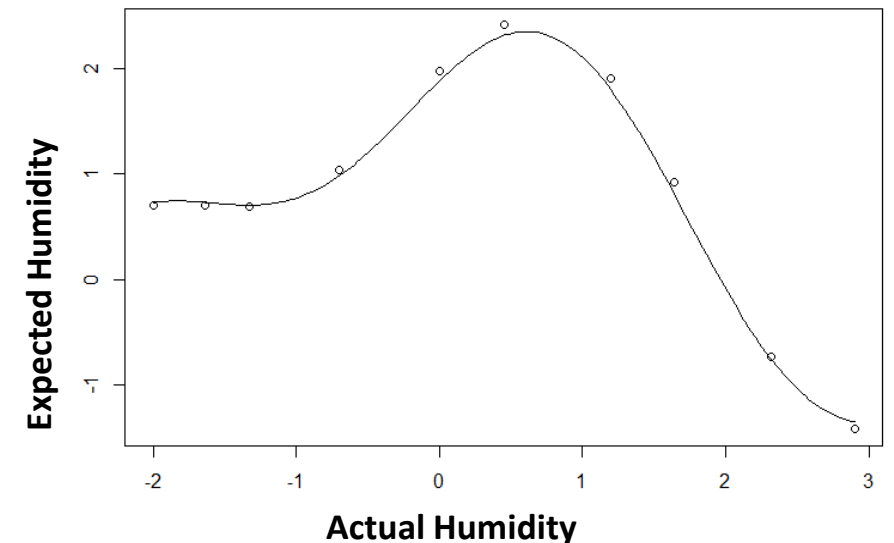
3. **Technical Approach:** description of the ideas, equations, algorithms used to solve the problem

The minimum of a function appears at one of its critical points

$\{s \in \mathbb{R} \mid f'(s) = 0\}$ . We find all the roots of  $f'$  and select the smallest one as the optimal watering time.

4. **Results:** figures showing qualitative and quantitative performance supported by discussion of what was successful and what fails

The method performs well as shown in Fig. 1. The performance could be improved if real-time humidity measurements are used to update  $f$ .



# Project Report: Examples

[https://natanaso.github.io/ref/Wang\\_LearningNavigation\\_SCR1\\_9.pdf](https://natanaso.github.io/ref/Wang_LearningNavigation_SCR1_9.pdf)

## Learning Navigation Costs from Demonstration via Differentiable Planning

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**Abstract**—This paper focuses on learning cost functions that capture desirable behavior in tasks demonstrated by an expert. In a task such as autonomous navigation in unknown environments, it is possible to obtain sequences of observations (e.g., images), states (e.g., poses), and control inputs but not direct queries of the underlying task-specific cost function. Hence, it is necessary to design a planning algorithm that, depending on the current cost representation, computes a control policy and propagates its error with respect to the demonstrations back to the cost representation. Our contribution is a probabilistic environment representation for local observation updates and cost function design, and a differentiable planning algorithm that performs state expansions only on a subset of promising states. Our complete model can be trained end-to-end and improves upon Value Iteration Networks and the Dyna-Q algorithm.

**Index Terms**—Inverse Reinforcement Learning, Differentiable Planning, Cost Learning

### I. INTRODUCTION

Autonomous robot systems increasingly require operation in unstructured, partially known, and dynamically changing environments. One core challenge for safe and robust navigation is that the true cost function of a navigation task, requiring safe, dynamically feasible, and efficient behavior, is generally not known while expert demonstrations can be utilized to uncover the underlying cost function [1], [2]. In addition, humans and animals can navigate successfully with partial knowledge of the environment and adapt when facing new obstacle configuration based on prior experience. Motivated by this observation, we focus on learning a cost function from demonstration that is not universally accurate over the state and control space but rather captures task-relevant information and leads to desirable behavior.

Our main contribution is an end-to-end differentiable model that combines a cost function representation and an efficient planning algorithm (see Fig. 1). The novelty of our approach is that the proposed model is fully differentiable, which allows using gradient-based optimization to improve the parameterized cost function. Our experiments show that the end-to-end differentiable model learns task-specific cost functions and improves upon Value Iteration Networks (VIN) [3] and the Dyna-Q algorithm [4] by handling partial and noisy observations. In summary, we offer the following contributions:

We gratefully acknowledge support from NSF CRII RI IIS-1755568.

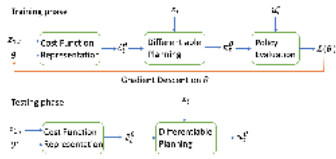


Fig. 1: Architecture for learning cost function representations from demonstrations via differentiable planning. During training, the goal is to learn a cost function parameterization  $\theta$  based on demonstrations, consisting of states  $x_{1:t}$ , controls  $u_{1:t}$ , and partial observations  $z_{1:t}$ , so that a control policy generated based on the learned cost incurs minimum loss  $\mathcal{L}(\theta)$ . Both the cost function representation  $\theta$  and the control policy  $\pi_\theta^*$  need to be differentiable with respect to  $\theta$  for error backpropagation. During testing in a new environment, online observations  $x_{1:t}$  and the trained parameters  $\theta^*$  provide the cost function necessary to generate a control policy.

- A cost function representation that incorporates a log-odds occupancy representation of the environment, updatable using a parameterized observation model.
- An efficient planning algorithm, which performs local convolutional operations encoding Bellman backups only on a subset of promising states. We guarantee that the output policy is differentiable with respect to the input cost function.
- An end-to-end differentiable model that learns task-specific cost functions from expert demonstrations by backpropagating policy performance loss through the planning algorithm and the cost representation.

### II. PROBLEM FORMULATION

Consider a robot navigating in an unknown environment with the task of reaching a goal state  $x_g \in \mathcal{X}$ . Let  $x_t \in \mathcal{X}$  be the discrete time robot state. For a given control input  $u_t \in \mathcal{U}$ , the robot state evolves according to known deterministic dynamics:  $x_{t+1} = f(x_t, u_t)$ . Let  $m^*$  be a function

## Adversarial Information Acquisition

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**Abstract**—This paper considers a non-cooperative two-player game modeling the problem of adversarial information acquisition in robotics. Each robot is equipped with a sensor, and is tasked with choosing control inputs that maximize an information (e.g. entropy) about the other player, while keeping its own state as uncertain to the other player as possible, subject to the available sensors. This adversarial information gathering problem has applications in surveillance, or search-and-rescue missions where the agent whose state is to be estimated may try to actively avoid the sensing robot. We formulate the problem of adversarial information acquisition, and provide an initial solution based on a variant of Monte Carlo Tree Search for simultaneous action games.

### I. INTRODUCTION

In this paper, we consider the problem of two robots interacting in an adversarial game where each robot attempts to estimate the state of its adversary, while keeping its own state hidden. This problem can have applications in search-and-rescue applications, where the agent to be found is mobile, and actively evades the sensing robot. In these problems, it is important to both accurately localize the target agent, while keeping one's own state hidden so that the target's ability to actively evade is reduced.

There is much prior work in the literature concerning the dynamics of pursuit-evasion in mobile robotic settings [3]. Approaches to the pursuit-evasion problem are split between considering the worst-case evader (adversary), and using probabilistic frameworks which consider the expected case. A common theme in the pursuit-evasion literature is the objective of reducing the distance to the evader to zero, or forcing the evader into a sensing footprint. In contrast, our problem is formulated using a probabilistic approach which optimizes an information theoretic quantity, namely entropy, about the distribution of the target to be tracked. Rather than closing distance to the target, our approach aims to produce the best estimate of the target's state, subject to the sensors available. Our previous work considers the information acquisition problem for target tracking [1], however this work assumes that the target being tracked moves independently of the sensing robot, and crucially is not trying to actively evade the sensing robot. In this work, the problem formulation is symmetric in the sense that the adversary is trying to maximize information gained about us, and also minimize the information we can gain about it.

We also draw attention to some biological inspiration for this problem. Motion camouflage [9] is a strategy utilized by dragonflies, which enables them to capture their prey by minimizing the optical flow of their motion. Mischiati and Krishnadas [8] consider the problem of mutual motion camouflage, where two agents each pursue each other, but attempt to maintain a constant bearing to avoid detection by the other agent. Our problem is related, but rather than considering pursuit-evasion, we consider the dynamics of an adversarial information gathering game.

In the most general case, the information acquisition game proposed is a stochastic game and is difficult to solve. McEneaney [7] discusses a class of stochastic games with finite-dimensional solutions and dynamic programming algorithms to solve them. With some assumptions on the motion and observation models of the agents in our game, the problem can be simplified to a deterministic game. McEneaney [6] introduces a curse-of-dimensionality free max-plus method for deterministic game problems, which is likely to be very applicable to the linear Gaussian version of the information-theoretic game introduced here. Additionally, Grinwald and Dawid [4] present a game-theoretic argument that maximizing entropy and minimizing worst-case expected loss are duals of each other. A comprehensive treatment on adversarial reasoning, is provided in the book by Kott and McEneaney [5]. The approach taken in this work is a variant of Monte Carlo Tree Search [11], for simultaneous action games. We present the details of this approach in Sec. III.

### II. PROBLEM FORMULATION

Consider a two-player partial information game with simultaneous moves. Each player  $i \in \{1, 2\}$  has a state  $x_{i,t}$  that evolves according to the following motion model:

$$x_{i,t+1} = f_i(x_{i,t}, u_{i,t}, w_{i,t}) \quad (1)$$

where  $u_{i,t} \in \mathcal{U}_i$  is a finite space of admissible moves (control inputs) and  $w_{i,t}$  is a random variable specifying the motion noise. Player  $i$  can observe its own state  $x_{i,t}$  and chooses its moves with the objective of tracking the evolution of the state of the other player. Each player is equipped with a sensor used to collect information about the other player according to the following observation model:

$$z_{i,t} = h_i(x_{i,t}, x_{j,t}, v_{i,t}) \quad (2)$$

[https://natanaso.github.io/ref/Lauri\\_MonteCarloTreeSearch\\_ICR\\_A15\\_Workshop.pdf](https://natanaso.github.io/ref/Lauri_MonteCarloTreeSearch_ICR_A15_Workshop.pdf)

## Active Object Recognition via Monte Carlo Tree Search

Mikko Lauri, Nikolay Atanasov, George J. Pappas, and Risto Ritala

**Abstract**—This paper considers object recognition with a camera, whose viewpoint can be controlled in order to improve the recognition results. The goal is to choose a multi-view camera trajectory in order to minimize the probability of having misclassified objects and incorrect orientation estimates. Instead of using offline dynamic programming, the resulting stochastic optimal control problem is addressed via an online Monte Carlo tree search algorithm, which can handle various constraints and provides exceptional performance in large state spaces. A key insight is to use an active hypothesis testing policy to select camera viewpoints during the rollout steps of the tree search.

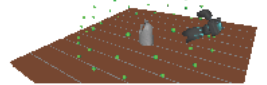


Fig. 1: Setup for the active object recognition problem. The camera position is restricted to a set of viewpoints (green) on a sphere centered at the object's location. The task is to choose a camera control policy, which minimizes the movement cost and the probability of misclassification.

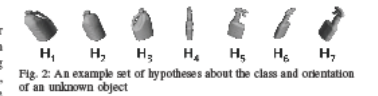


Fig. 2: An example set of hypotheses about the class and orientation of an unknown object

### I. INTRODUCTION

The goal of this paper is to choose a sequence of views for an RGB-D camera in order to identify the class and orientation of an object of interest (see Fig. 1). Unlike many existing approaches, which consider a next-best-view problem [1], [2], [3], we plan a multi-view camera trajectory to minimize the probability of having misclassified objects and incorrect orientation estimates. In previous work [4], we addressed a similar stochastic optimal control problem by casting it as a partially-observable Markov decision process. A point-based approximate solver [5] was used to obtain a non-greedy policy offline. Since repeated observations of the object from the same viewpoint provide redundant information, it is desirable to disallow viewpoint revisiting. The drawback of computing a policy offline is that revisiting and occlusion constraints are hard to incorporate and if the environment were to change, the computed policy would no longer be useful. The idea of this paper is to apply Monte Carlo tree search (MCTS, [6], [7]) to the active object recognition problem. MCTS is a best-first online planning approach which can handle various constraints and has exceptional performance in large challenging domains such as game solving [8], [9] and belief-space planning in robotics [10], [11], [12].

Offline, a 3-D model database is used to train a viewpoint-pose tree [4] by extracting point clouds from views on a sphere around each model. A set of Fast Point Feature Histograms [13] is extracted from each point cloud and the clouds are arranged in a tree structure according to their feature similarity (see [4] for details). Given a query point cloud, the best-matching cloud from the tree carries information about the class and orientation of the observed object and about the quality of the feature match. Thus, the tree provides an observation  $x_t \in \mathcal{Z}$ , consisting of the class, orientation, and confidence score of the top match. The model database is used to learn the probability density function (pdf)  $q(\cdot | x_t, H_t)$  of  $z$  conditioned on any camera viewpoint  $c \in \mathcal{X}$  and any hypothesis  $H_t$ ,  $i = 1, \dots, M$ .

### II. PROBLEM FORMULATION

**Problem.** Given a camera pose  $x_0 \in \mathcal{X}$ , a prior  $p_0 \in [0, 1]^M$  on the true hypothesis  $H_{*}$ , and a planning horizon  $T < \infty$ , choose a sequence of functions  $\mu_t : (\mathcal{Z} \times \mathcal{X})^{t+1} \rightarrow \mathcal{X}$  for  $t = 0, \dots, T-1$ , which minimizes the average movement cost and the probability of an incorrect hypothesis:

$$\min_{\mu_{0:T-1}} \frac{1}{T} \sum_{t=1}^T g(x_{t-1}, x_t) + \lambda P_e(T) \quad (1)$$
$$\text{s.t. } x_{t+1} = \mu_t(x_{0:t}, x_{0:t}), \quad t = 0, \dots, T-1,$$
$$x_{t+1} \notin \{x_0, \dots, x_t\}, \quad t = 0, \dots, T-1,$$
$$x_t \sim q(\cdot | x_t, H_t), \quad t = 0, \dots, T,$$
$$p_t = b(p_{t-1}, z_t, x_t), \quad t = 1, \dots, T,$$

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N. Atanasov and G. Pappas are with GRASP Lab, University of Pennsylvania, Philadelphia, PA 19104, USA. {natanasov, pappasg}@seas.upenn.edu. This work was supported by Teramem, one of six centers of STARnet, a Semiconductor Research Corporation program sponsored by MARCO and DARPA.

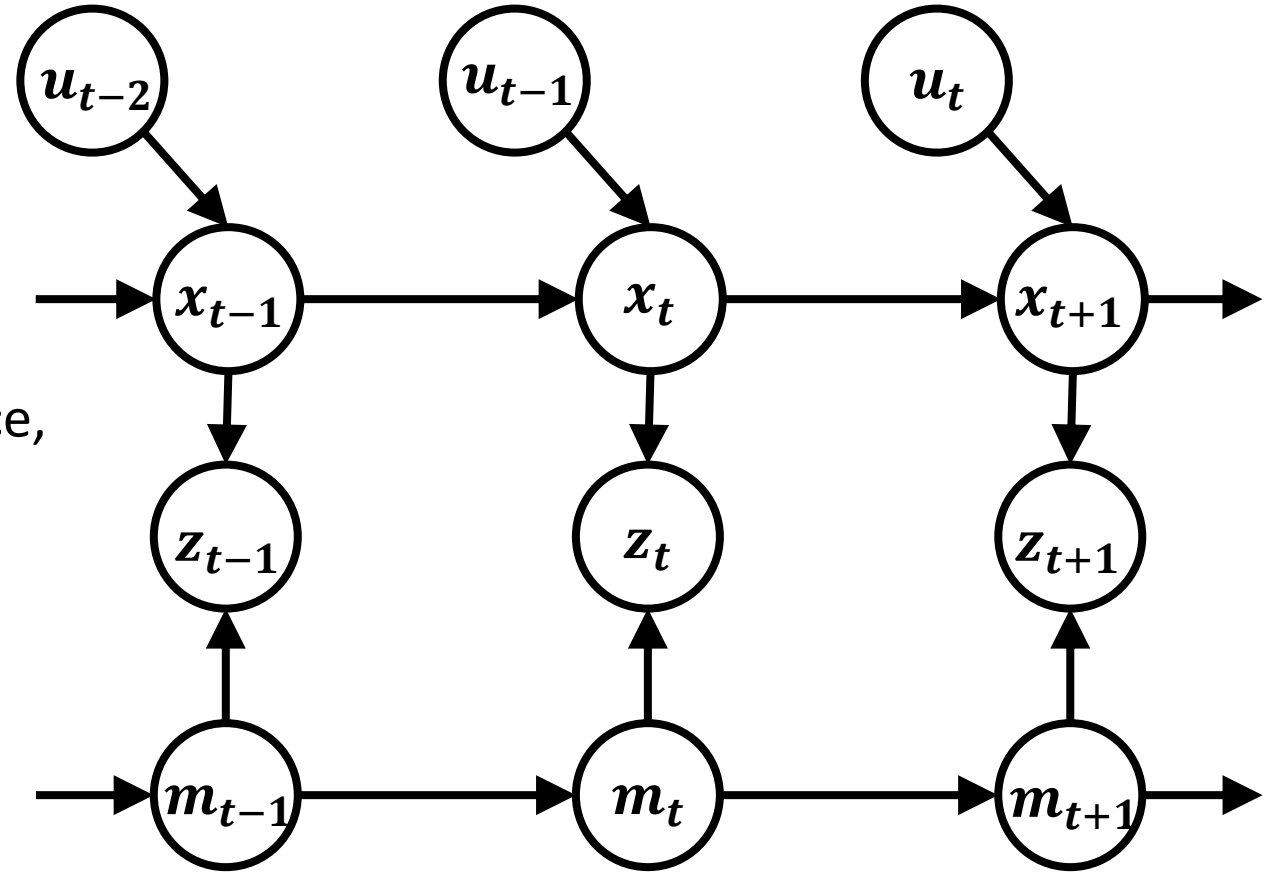
<sup>1</sup>After a hypothesis is chosen, the discrete orientation estimate can be refined by aligning the observed object surface to the corresponding model in the training database, e.g. by using the iterative closest point algorithm.

# Syllabus

Date	Lecture	Material	Assignment
Jan 09	Introduction	Matrix-calculus	
Jan 11	Unconstrained Optimization	Barfoot-Ch.4.3.1	
Jan 16	Rotations	Barfoot-Ch.6.1-6.3	
Jan 18	Robot Motion and Observation Models	Barfoot-Ch.6.4	HW1
Jan 23	Catch up		
Jan 25	Localization and Odometry from Point Features		PR1
Jan 30	Matrix Lie Groups	Barfoot-Ch.7.1-7.2	
Feb 01	Matrix Lie Group Optimization	Barfoot-Ch.7.1-7.2	
Feb 06	Catch up		
Feb 08	Bayes Filter	Barfoot-Ch.4.2	HW2
Feb 13	Particle Filter	Thrun-Burgard-Fox-Ch.7-9	PR2
Feb 15	Particle Filter SLAM	Thrun-Burgard-Fox-Ch.7-9	
Feb 20	Catch up		
Feb 22	Kalman Filter	Barfoot-Ch.3.3, Sarkka-Ch4	
Feb 27	EKF, UKF	Barfoot-Ch.4.2, Sarkka-Ch5	HW3, PR3
Mar 01	Visual-Inertial SLAM		
Mar 06	Visual Features, Optical Flow	Image-Features	
Mar 08	TBD		
Mar 13	TBD		
Mar 15	TBD		
Mar 20	Final Exam		

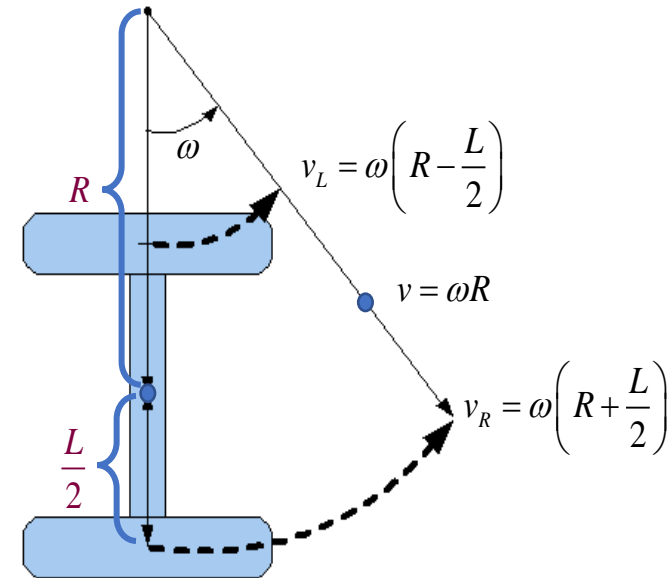
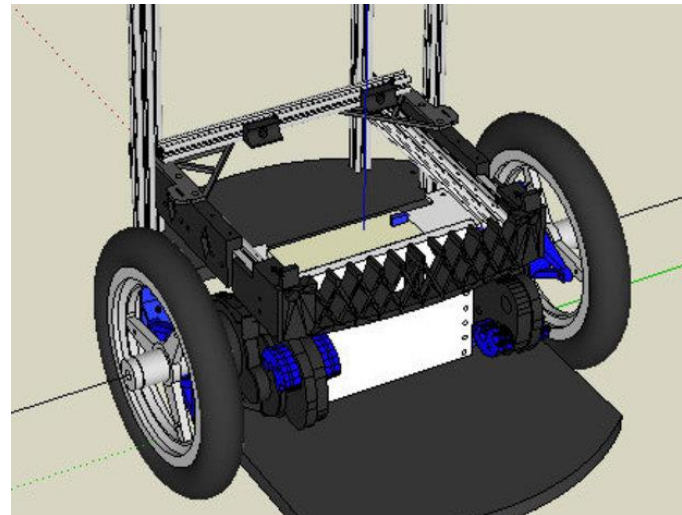
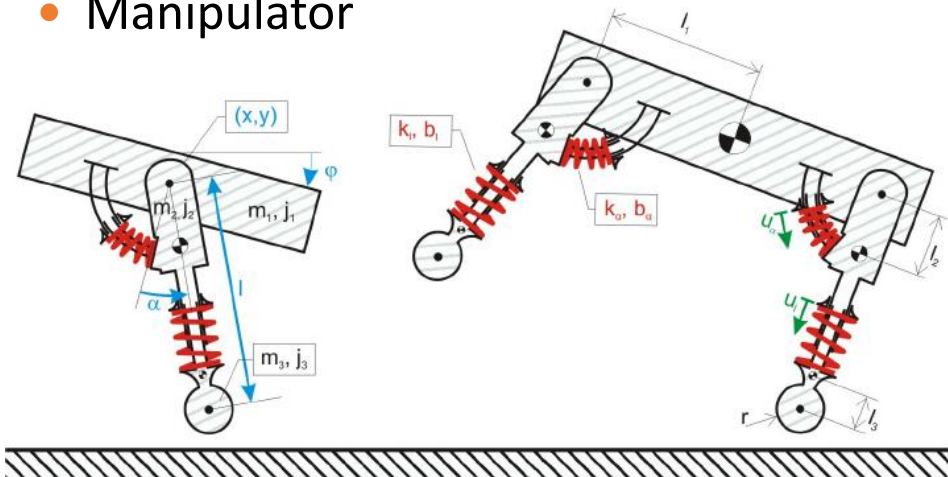
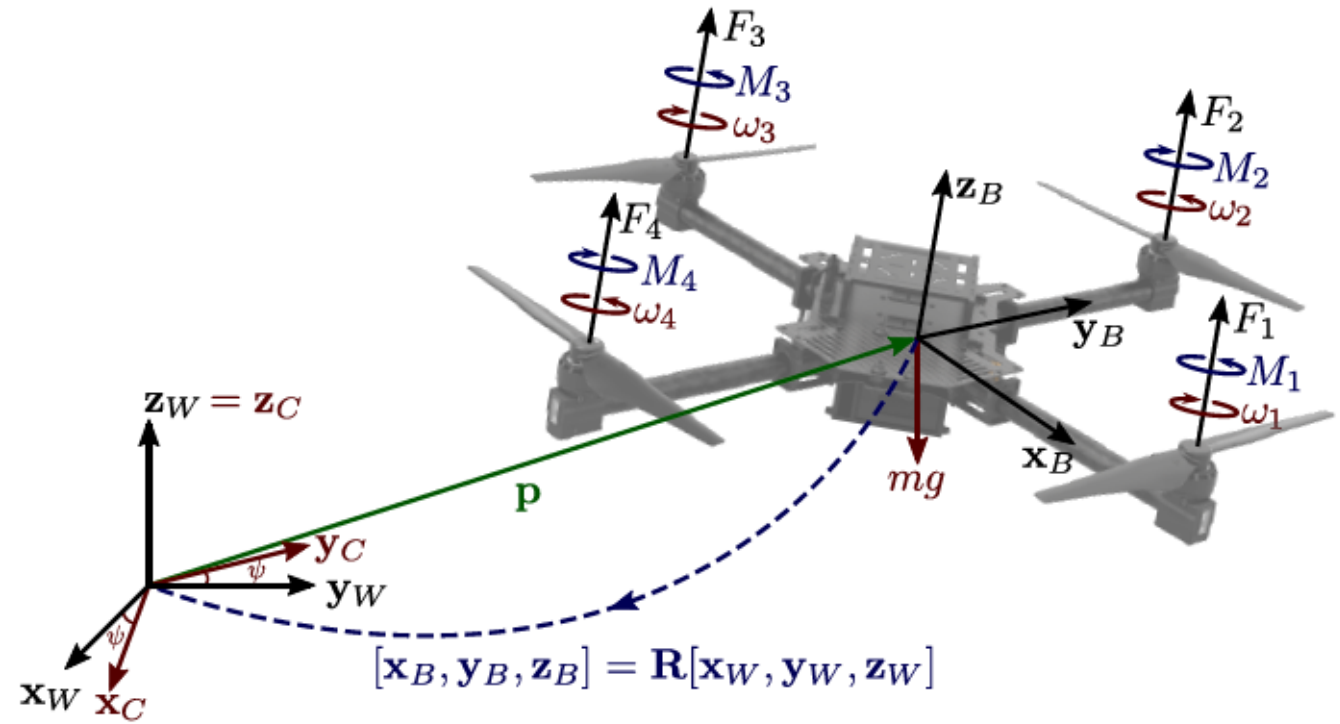
# Structure of Robotics Problems

- **Time:**  $t$  (discrete or continuous)
  - **Robot state:**  $x_t$  (e.g., position, orientation, velocity)
  - **Environment state:**  $m_t$  (e.g., map of free space, locations of objects)
  - **Control input:**  $u_t$  (e.g., quadrotor thrust and torque)
  - **Observation:**  $z_t$  (e.g., image, laser scan, radio signal, inertial measurements)
- 
- **Motion Model:**  $p(x_{t+1}|x_t, u_t)$  --- describes the motion of the robot to a new state  $x_{t+1}$  after applying control input  $u_t$  at state  $x_t$
  - **Observation Model:**  $p(z_t|x_t, m_t)$  --- describes the observation  $z_t$  of the robot depending on its state  $x_t$  and the map  $m_t$  of the environment



# Motion Models

- A motion model describe the kinematics or dynamics of the robot state  $x_t$
- Wheeled robots:
  - Differential drive (roomba)
  - Ackermann drive (car, bicycle)
- Aerial robots:
  - Fixed-wing aerial vehicle
  - Quadrotor aerial vehicle
- Legged and humanoid robots:
  - Quadruped
  - Manipulator





# Observation Models

- **Position Sensor:** directly measures position (e.g., GPS, laser scanner, IR sensor, RGBD camera)
- **Velocity/Acceleration/Force Sensor:** measures linear acceleration or angular velocity or pressure or force (accelerometer, gyroscope, inertial measurement unit (IMU), tactile sensor)
- **Bearing Sensor:** measures angles (e.g., magnetometer, camera, microphone)
- **Range Sensor:** measures distances (e.g., radio)



FLIR RGB Camera



VectorNav IMU



Ublox GPS  
and Compass



Beaglebone  
Radio



Intel RealSense  
RGBD Camera



Garmin Single-beam Lidar



Hokuyo  
2D Lidar



HDL-64E



HDL-32E

Velodyne  
3D Lidar



VLP-16

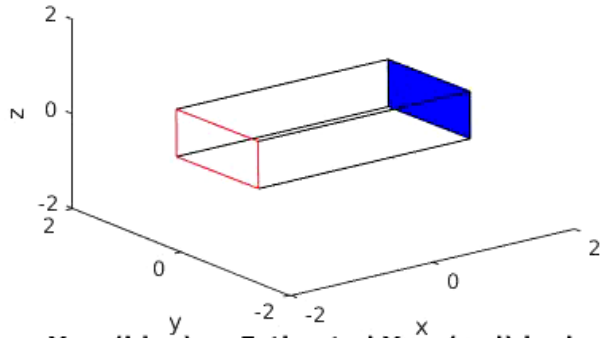


Hex 6-Axis  
Force/Torque  
Sensor

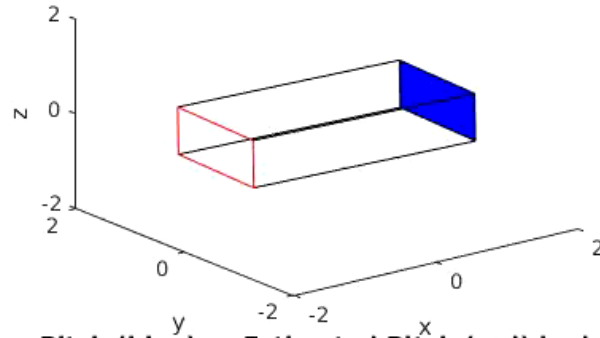
# Project 1: Orientation Tracking

- Use constrained gradient descent to track the 3D orientation of a rotating body using IMU measurements and construct a panorama using RGB images

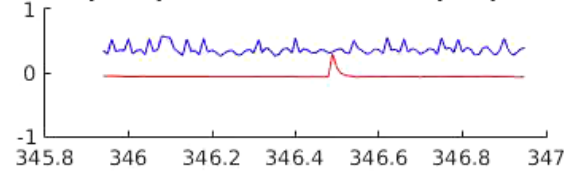
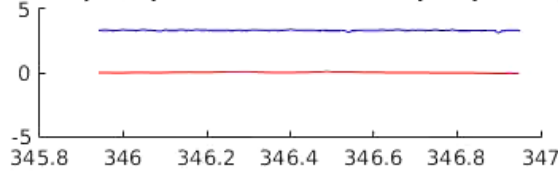
$\text{grav} = [-0.00, -0.00, 0.01]$   
 $\text{yaw} = -0.24, \text{pitch} = -0.06, \text{roll} = 0.31$



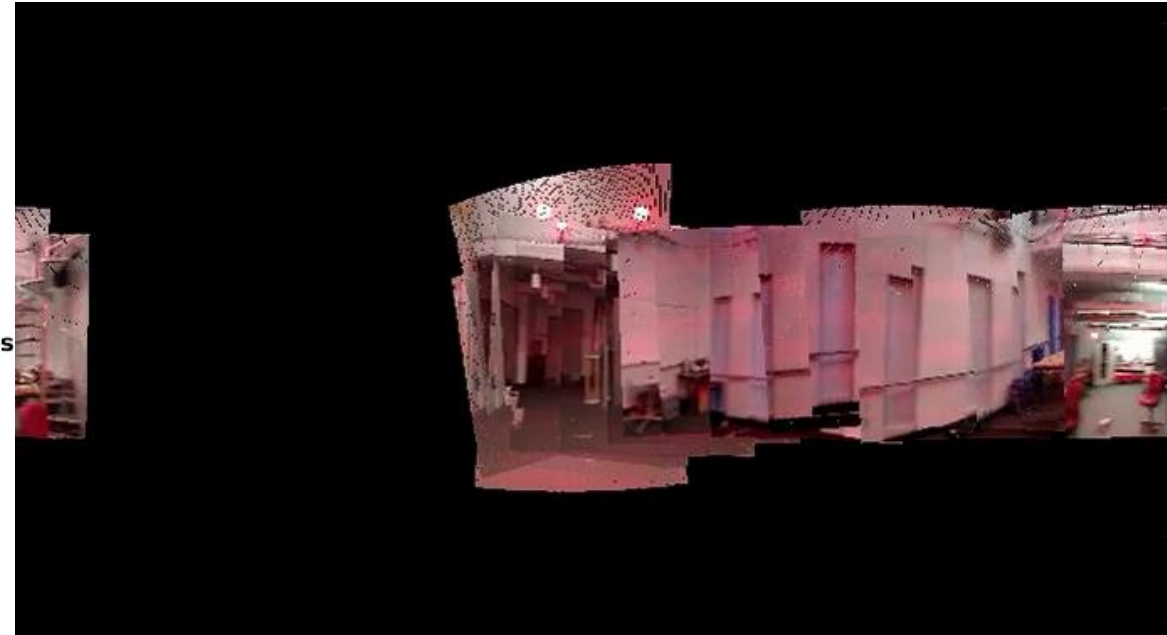
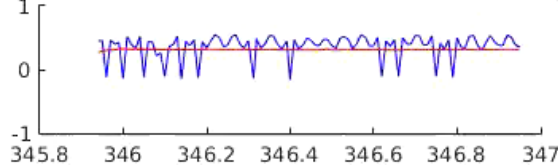
$\text{grav} = [-0.00, -0.01, 1.01]$   
 $\text{yaw} = 3.35, \text{pitch} = 0.37, \text{roll} = 0.39$



**True Yaw (blue) vs Estimated Yaw (red) in degrees** **True Pitch (blue) vs Estimated Pitch (red) in degrees**



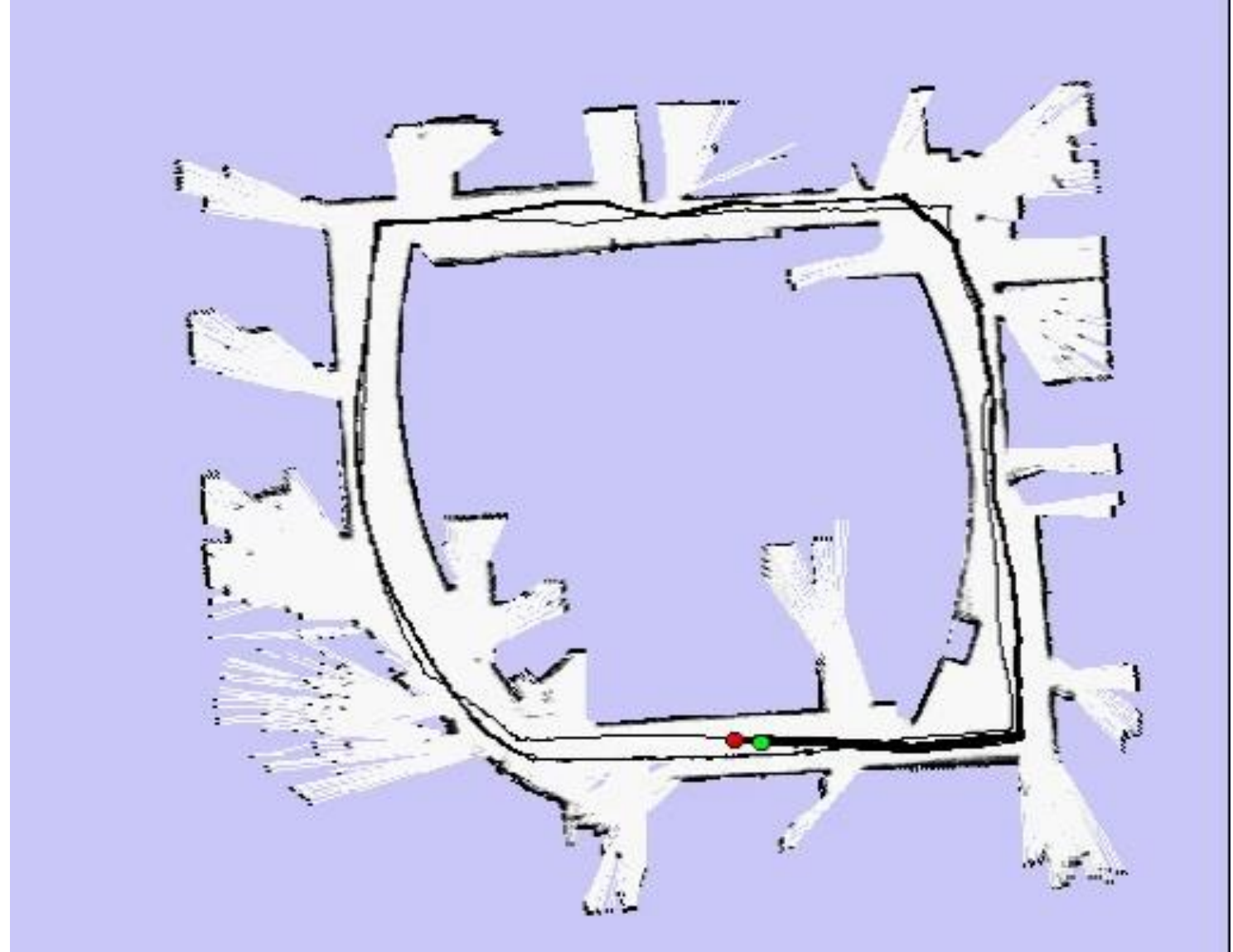
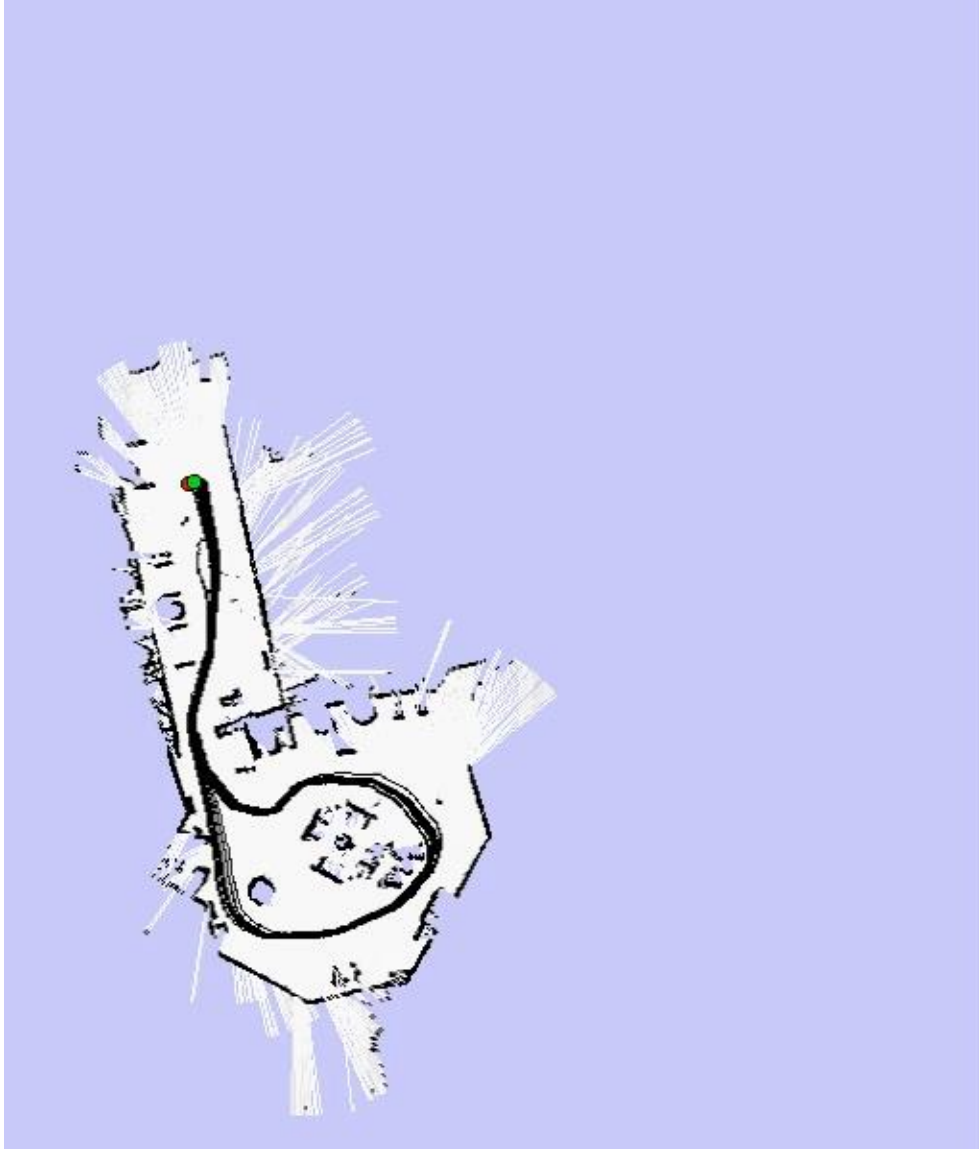
**True Roll (blue) vs Estimated Roll (red) in degrees**



## Project 2: Particle Filter SLAM

Montemerlo et al., FastSLAM, AAAI'02

- Simultaneous localization and mapping (SLAM) using a lidar scanner



# Project 3: Visual Inertial SLAM

Mur-Artal et al., OrbSLAM, IEEE T-RO'15

- Kalman filter tracking of the 3D pose of a moving robot based on IMU and camera measurements



TRACKING - KFs: 456 , MPs: 34546 , Tracked: 353

